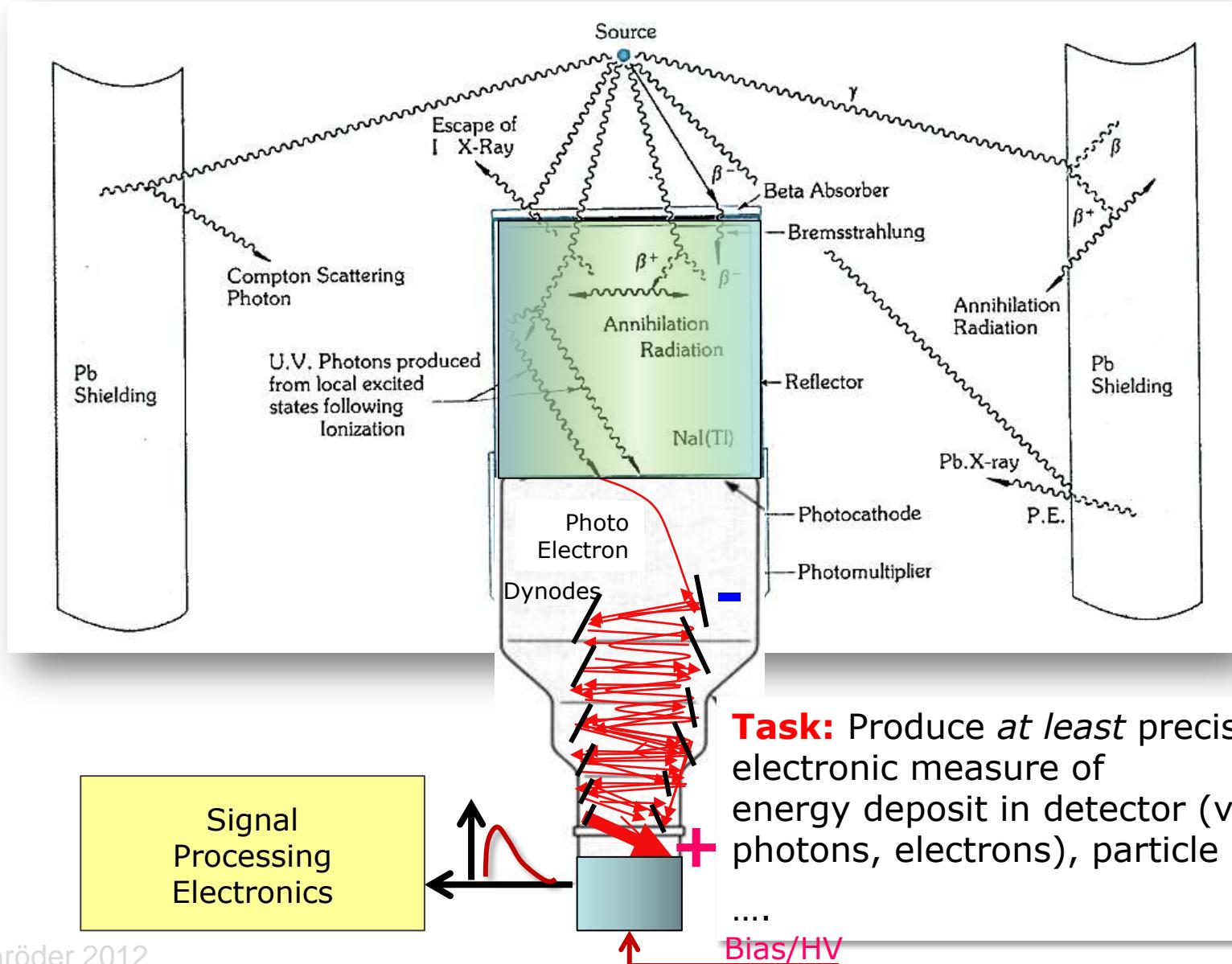


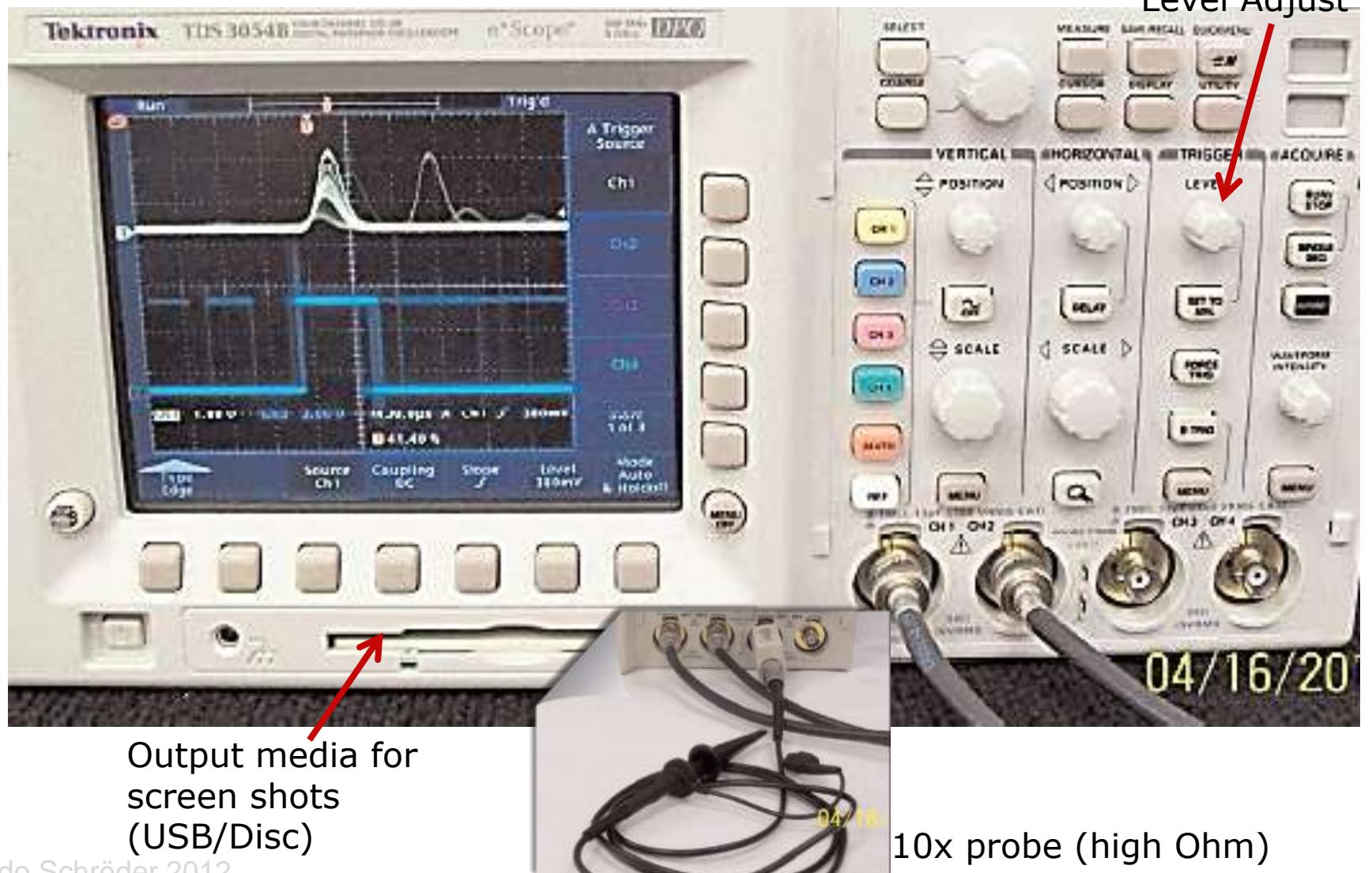
Intro to Electronic Signal Processing



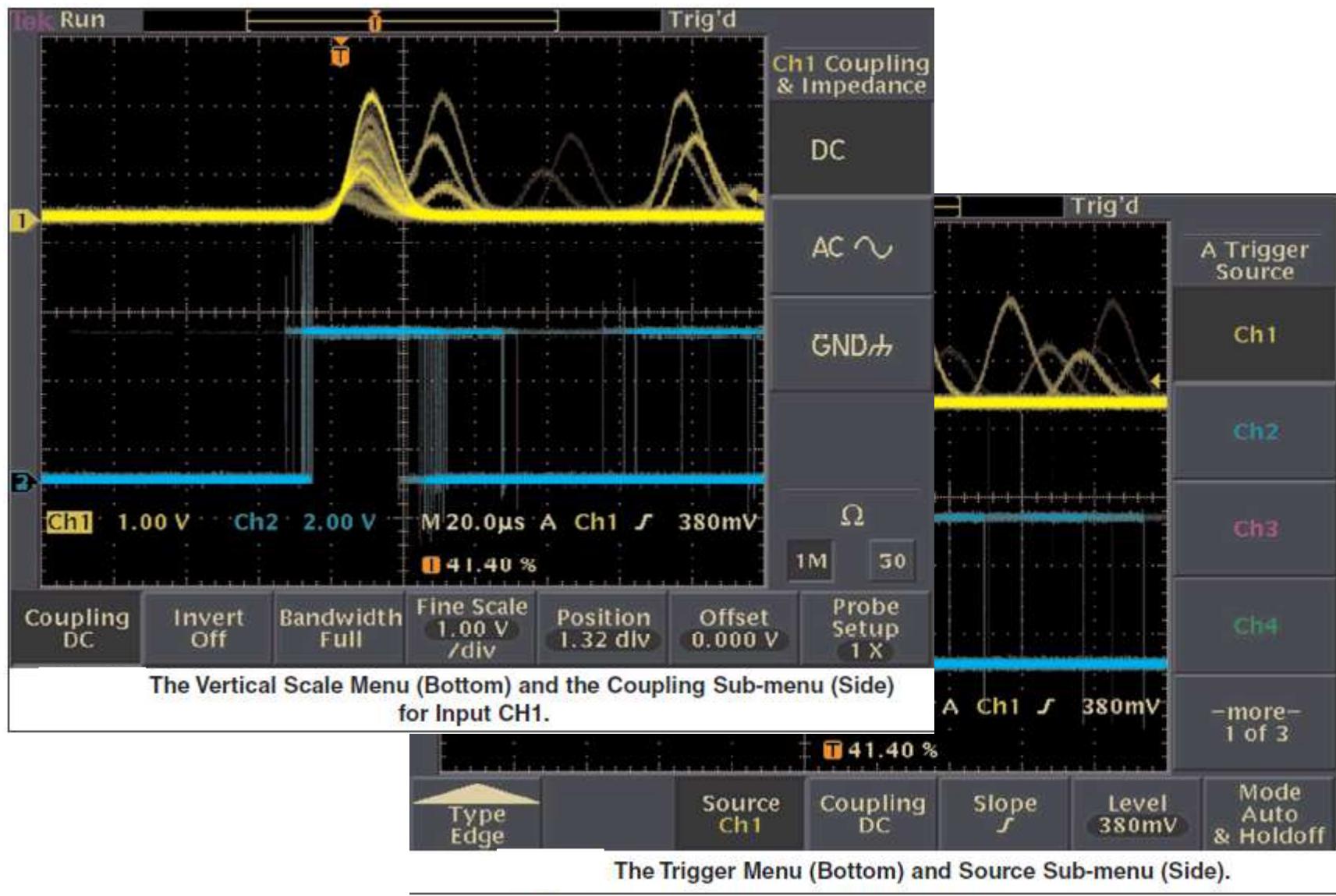
Detector Response to Radiation



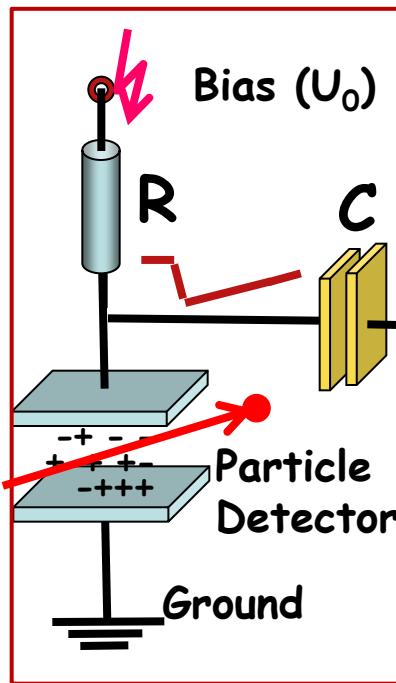
Digital Sampling Oscilloscope



Scope Screen Shots



Basic Radiation Detection/Counting System

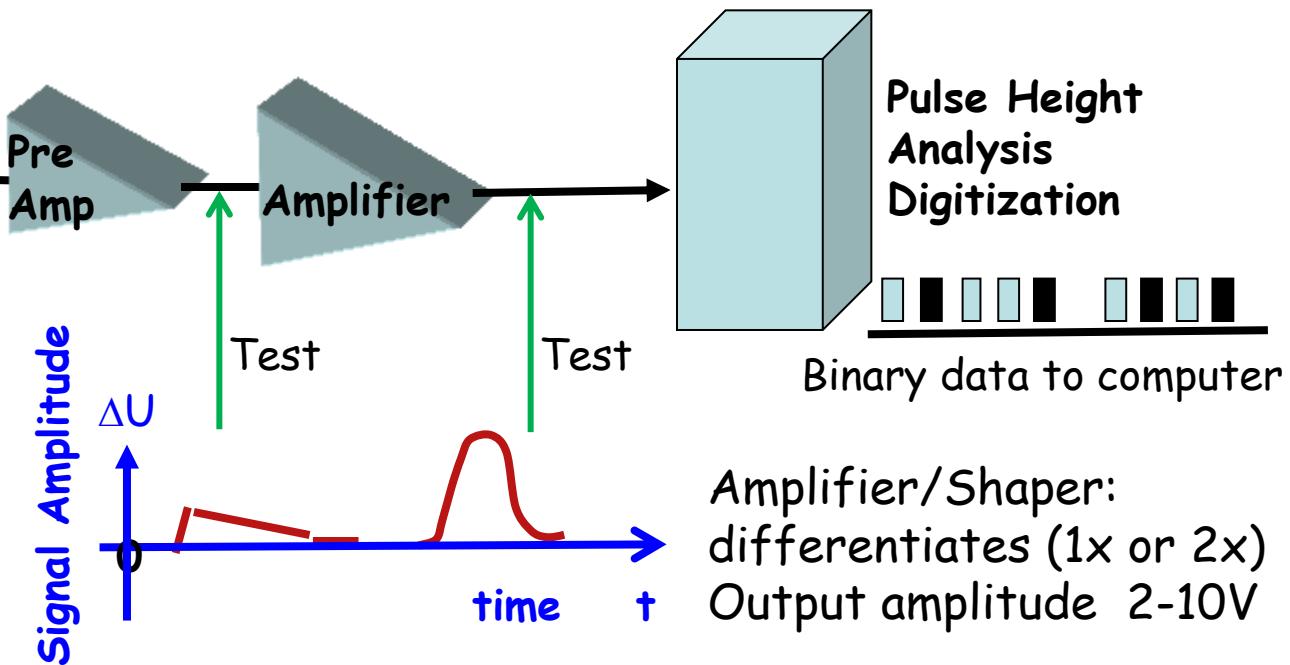


R : Load resistor

C : Insulates
electronics
from HV bias.

Pulse height 20-100 mV

Charge sensitive preamplifier: Voltage output pulse height ($\sim 0.1V$), dependent on detector and radiation.



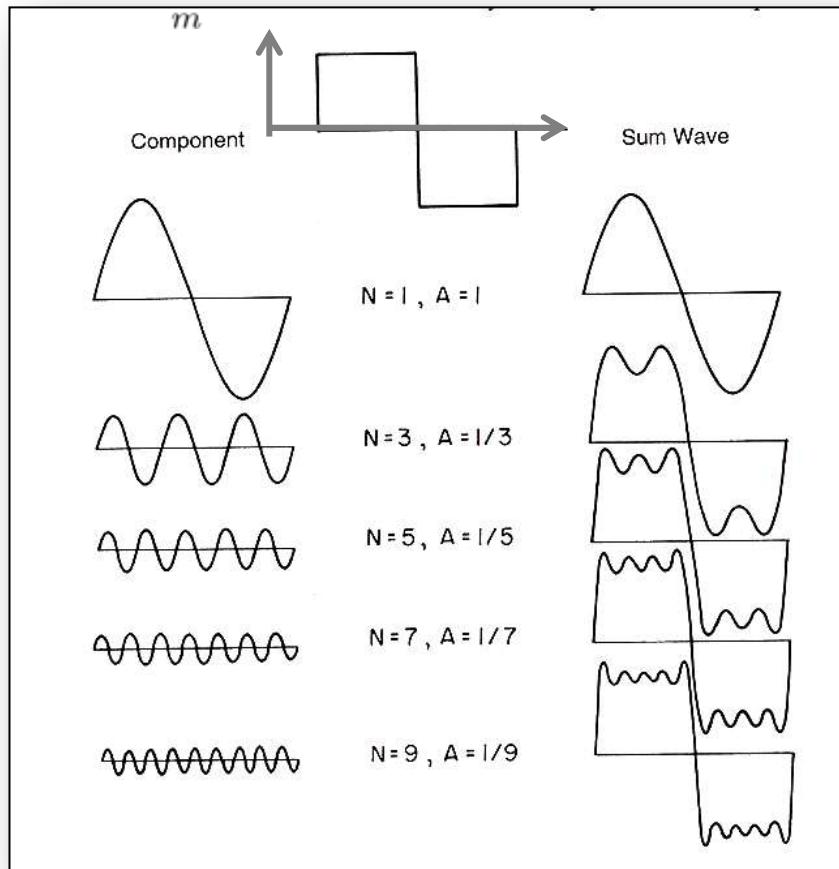
Amplifier/Shaper:
differentiates (1x or 2x)
Output amplitude 2-10V

Interaction of radiation with detector
temporarily ionizes medium
→ time (frequency) dependent change ΔU
in electric potential at collector electrodes,
transmitted as elec. Wave $g(t) \sim f(\omega)$.

Time and Frequency Domains

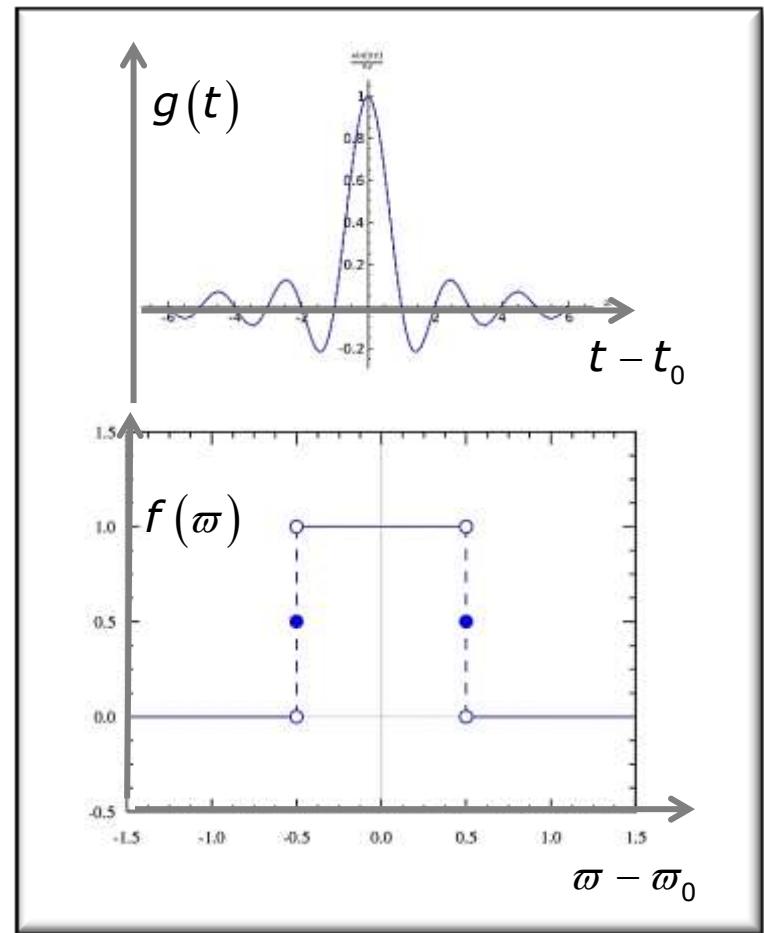
Fourier Series: adding harmonic components. Example $A_m=1/m$, $B_m=0$

$$f(t) = \sum_m [A_m \sin(2\pi mft) + B_m \cos(2\pi mft)]$$



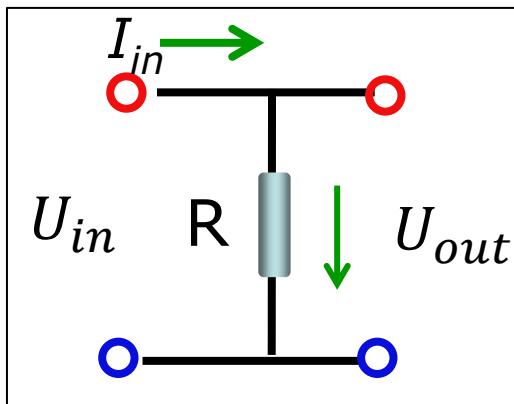
Fourier Transforms: adding continuous frequency spectrum components.

$$f(\varpi) = (2\pi)^{-1/2} \int g(t) \exp[i\varpi t] dt$$



Time dependent signals processed by frequency dependent electronics

Passive Electronic Circuit Components

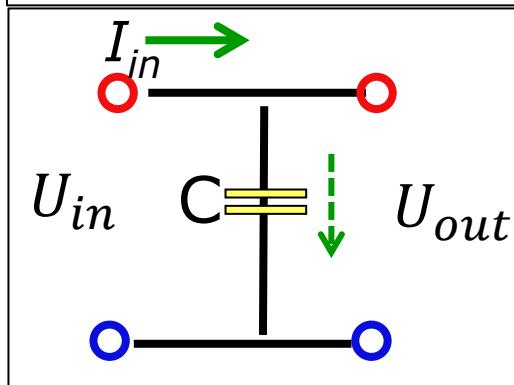


Assume no load on output ($R_{out} \rightarrow \infty$)

$$U_{out} = I_{in} \cdot R = U_{in} \rightarrow Z_R := R = U_{in}/I_{in}$$

Current flows continuously (DC or AC voltage)

$$U_{out}(t) = I_{in}(t) \cdot Z_R = U_{in}(t), \text{ Impedance } Z_R$$

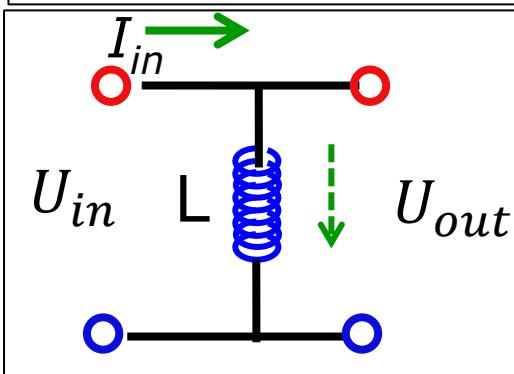


Current flows only until C is charged to $Q = C \cdot U_{in}$

$$I = \frac{dQ}{dt} = C \cdot \frac{dU_{in}}{dt} \rightarrow I = 0 \text{ for } U_{in} = \text{const}$$

$$U_{in}(t) = U_0 \cdot e^{i\omega t} \rightarrow I(t) = (i\omega C) \cdot U_{in}(t)$$

$$\text{Impedance } Z_C := U_{in}(t)/I(t) = (i\omega C)^{-1} \xrightarrow{\omega \rightarrow \infty} 0$$

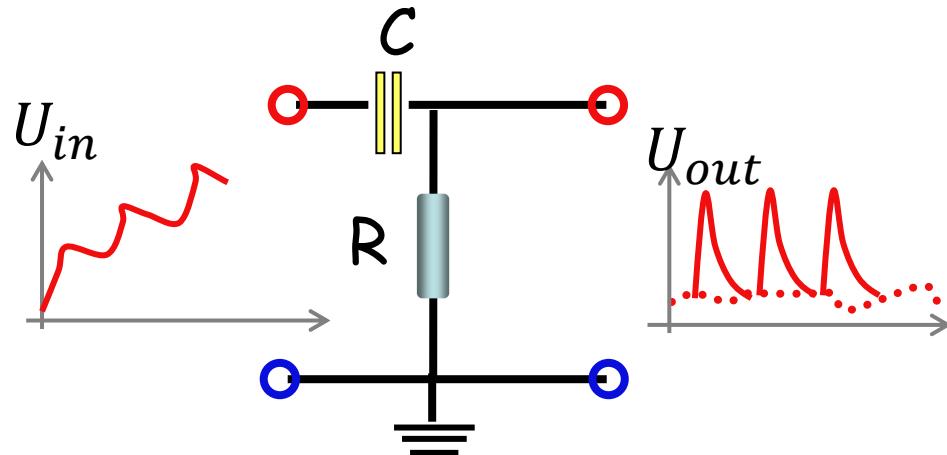


Inductance L makes a short circuit for $U_{in} = \text{const.} \rightarrow U_{out} = 0$. But for AC current/voltage

$$I_{in}(t) = I_0 \cdot e^{i\omega t} \rightarrow U_{out} = -L \frac{dI_{in}}{dt} = -(i\omega L) \cdot I_{in}(t)$$

$$\text{Impedance } Z_L := U_{in}(t)/I(t) = (-i\omega L) \xrightarrow{\omega \rightarrow \infty} \infty$$

Electronic Circuit Components

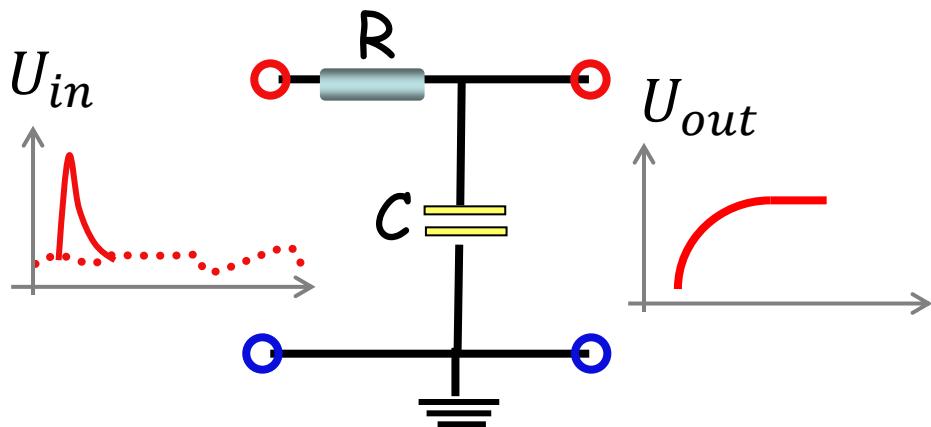


Differentiator (high pass)

$$U_{out} = \frac{R}{R + Z_C} U_{in}$$

$$\omega \rightarrow \infty: Z_C \rightarrow 0, U_{out} = U_{in}$$

Output images rapid changes
of input signal $U_{out} \propto dU_{in}/dt$



Integrator (low pass)

$$U_{out} = \frac{Z_C}{R + Z_C} U_{in}$$

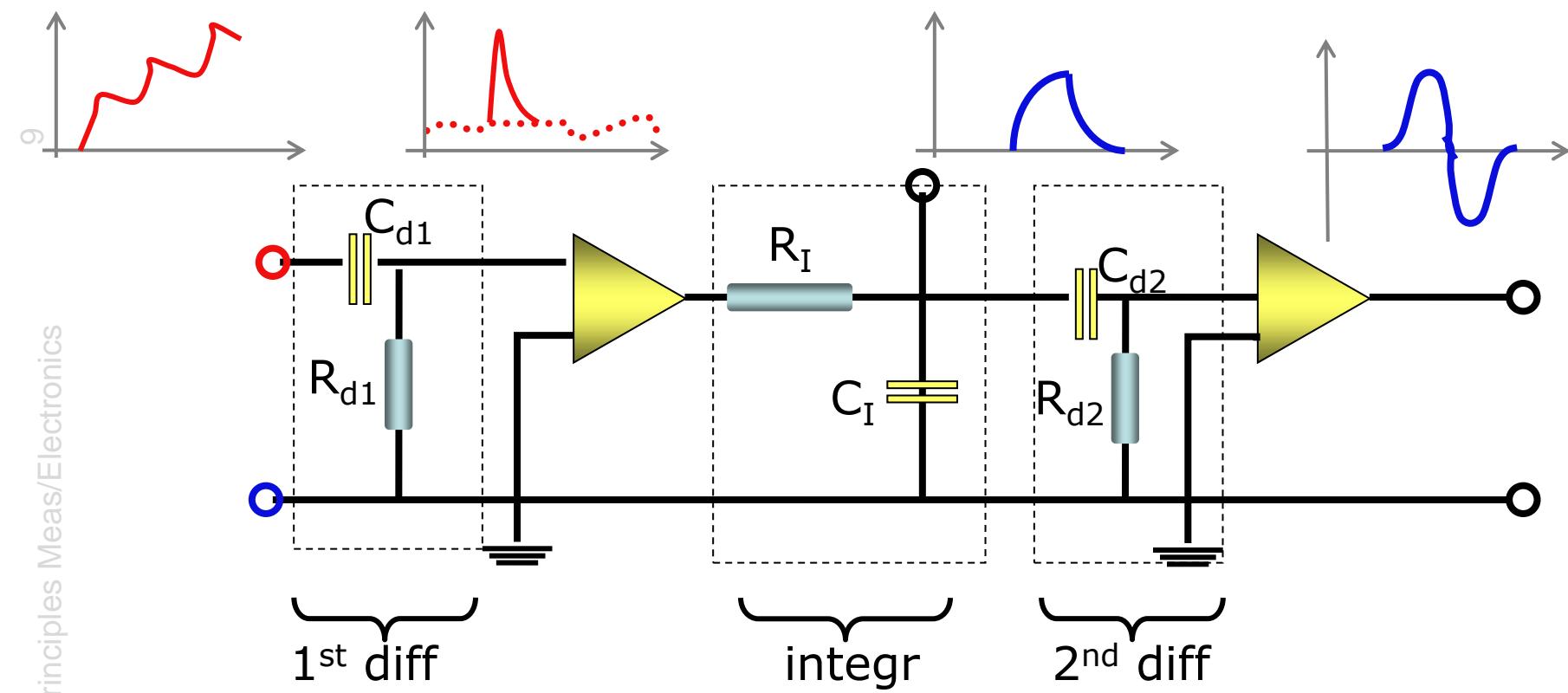
$$\omega \rightarrow 0: Z_C \rightarrow \infty, U_{out} = U_{in}$$

Filters out fast changes
of input signal, smoothens input
 $U_{out} \propto \int U_{in} dt$

Combination of differentiators + integrators makes selective filter
("band pass")

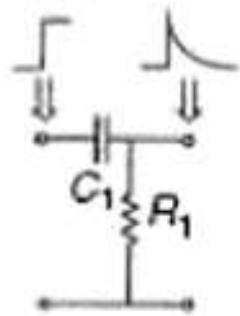
Main/Shaping Amplifiers

- Tasks: 1) Linear amplification to pulse heights of $U \approx (1-10)V$
2) Improvement of signal/noise ratio (integration)
3) Pulse shaping (Gaussian shape is best)

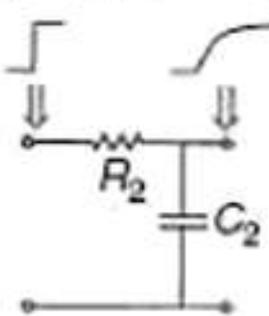


CRRC Pulse Shaping

(a) Differentiation
(high-pass filter)

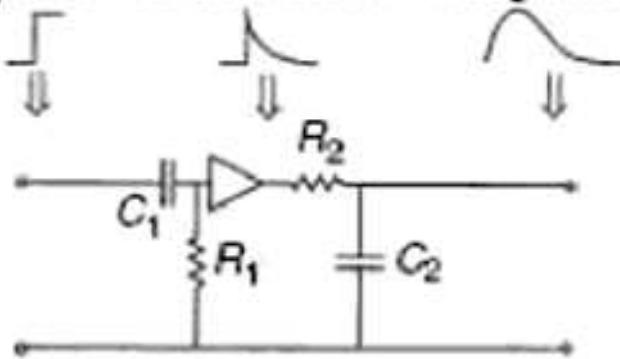


(b) Integration
(low-pass filter)



(c) Combined CRRC circuit

Input pulse After differentiation After integration



Pulse shape

Relative
'noise'



1.00



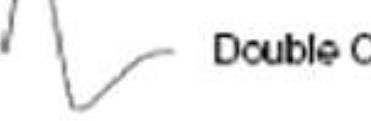
1.08



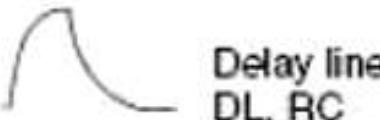
1.12



$\begin{cases} 1.36, n=1 \\ 1.22, n=2 \\ 1.18, n=3 \\ 1.12, n=\infty \end{cases}$

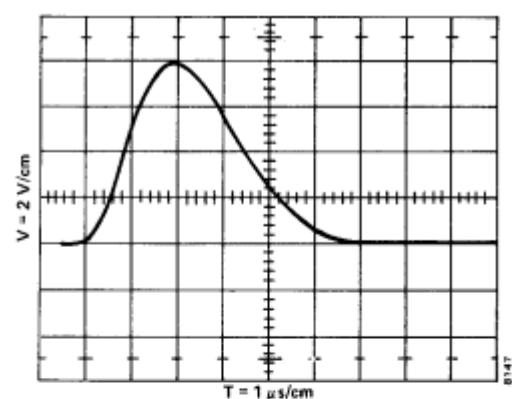


1.88

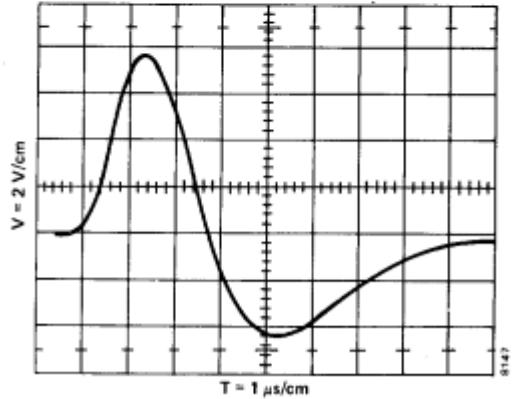


1.10–1.41

Main/Spectroscopy Amplifiers



Correct Amplifier Unipolar Output.



Correct Amplifier Bipolar Output.

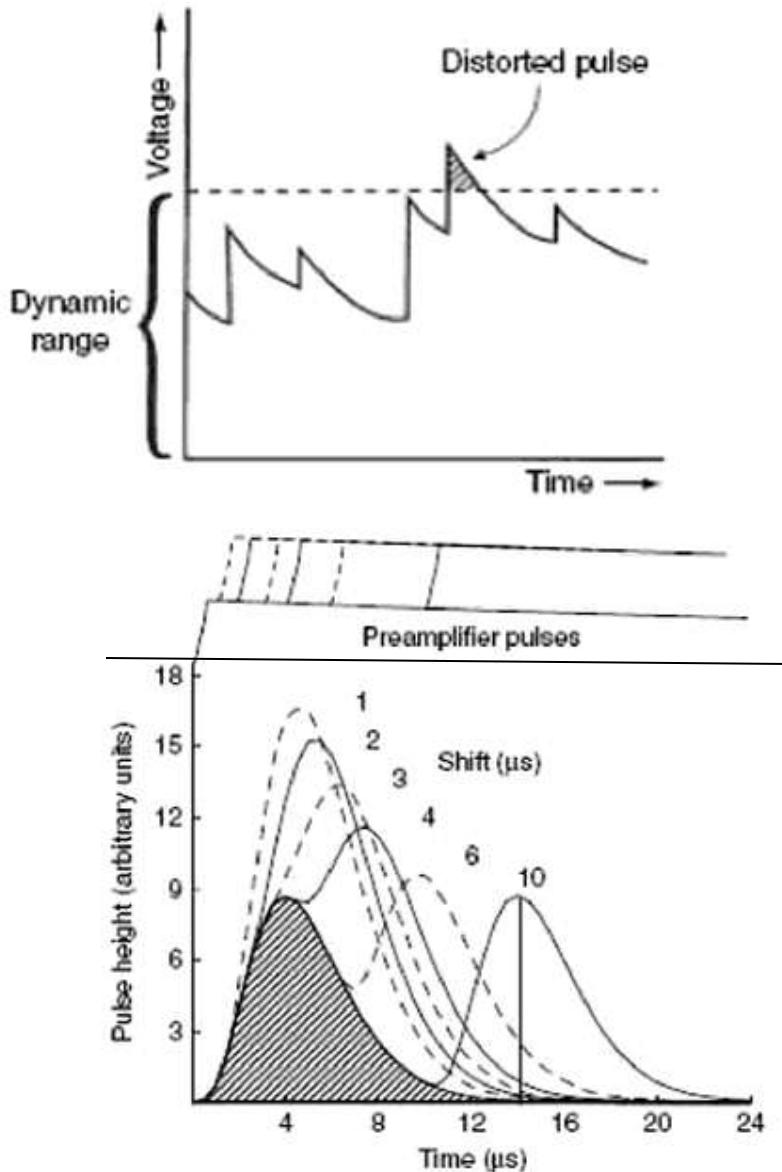


Tasks: Generate signal with amplitude **proportional** to collected detector charge. Needs absolute calibration of pulse amplitude.



← Preamp
Power

Effects of Pile-Up

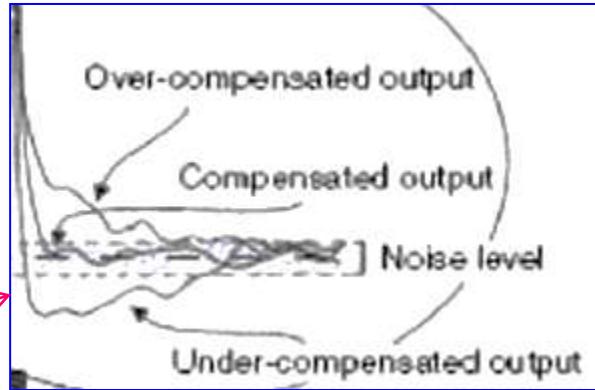
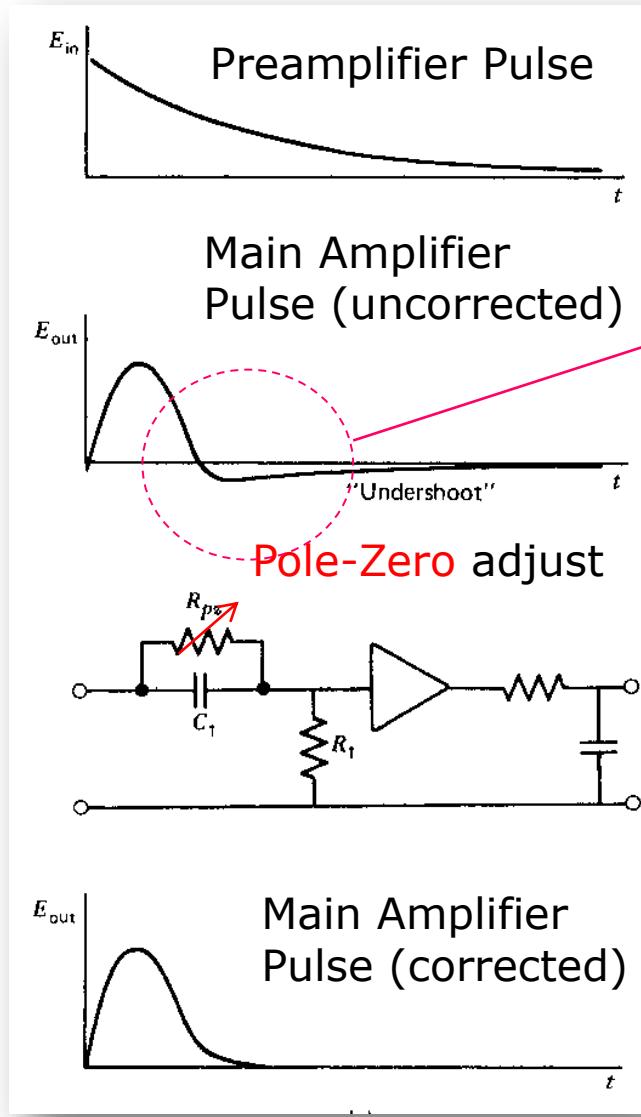


High count rate (relative to pulse length/decay time) can lead to pile up
→ from small non-linearities to serious distortions, line shapes “ghost lines”

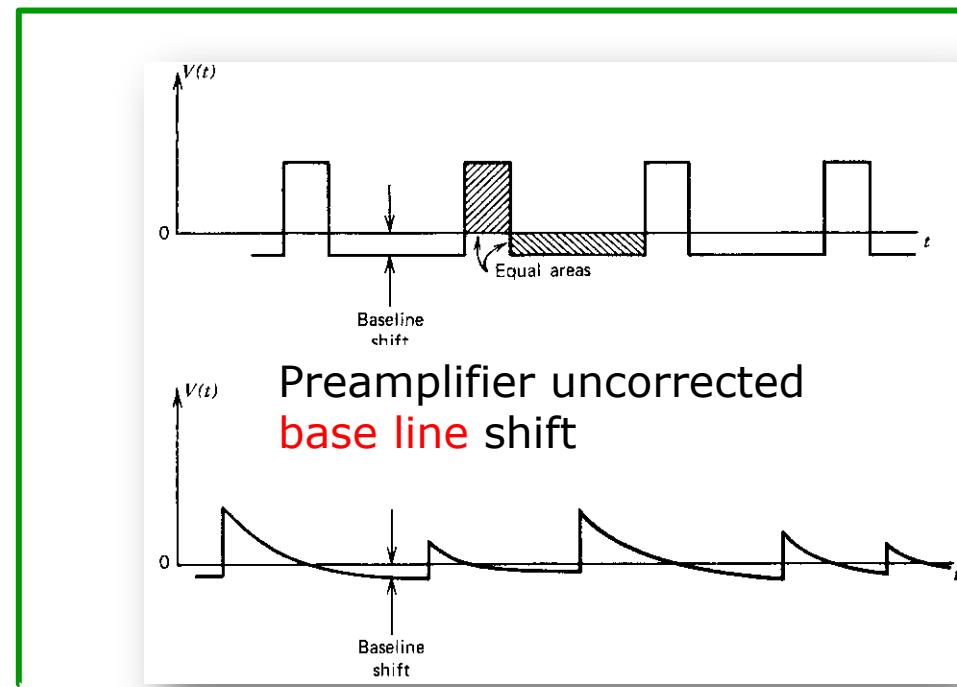
Artificial test of the pile-up effect. Successive signals add on to each other, creating an effectively non-zero base line.

Avoid by reducing signal rate or width (pulse decay time)

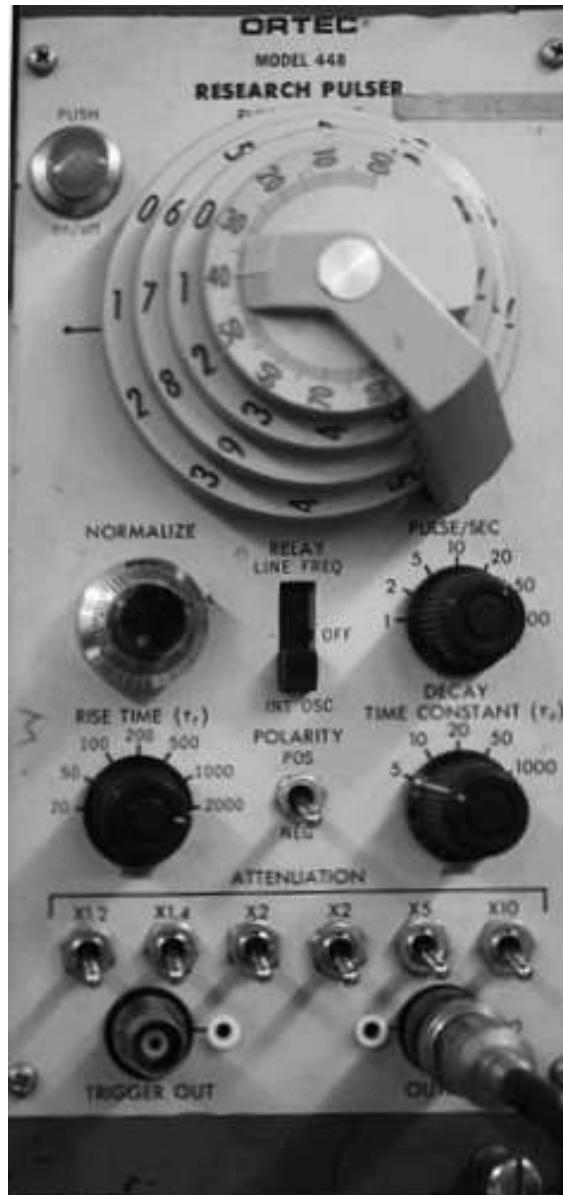
Pole-Zero & Base Line Shift Distortions



Blow-up of pulse
under/over shoot



Test Modules: Precision Pulse Generators



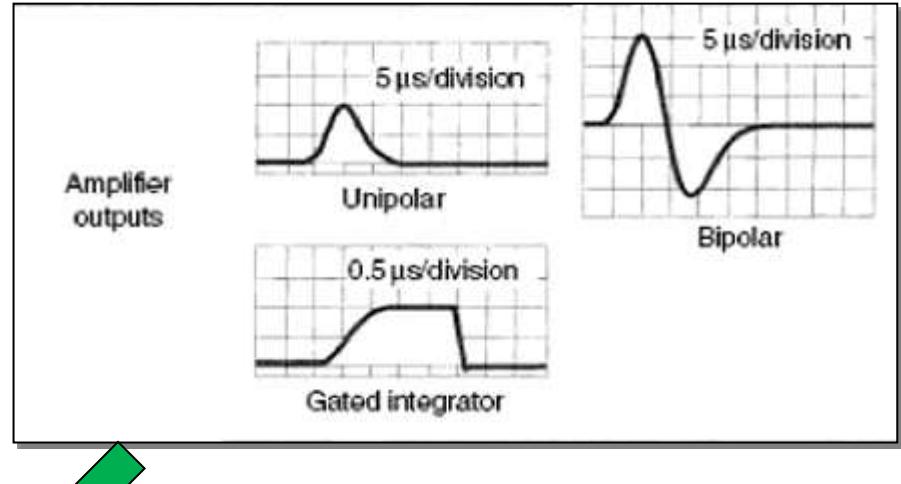
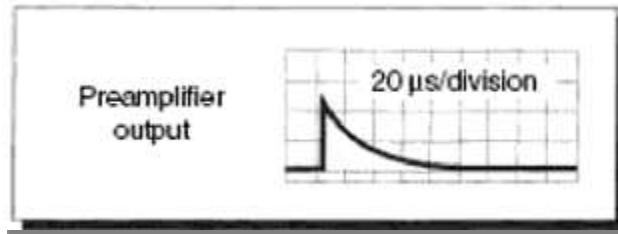
Tasks:

Simulate signals of physical events, controlled pulse shape, amplitude, timing, repetition rate

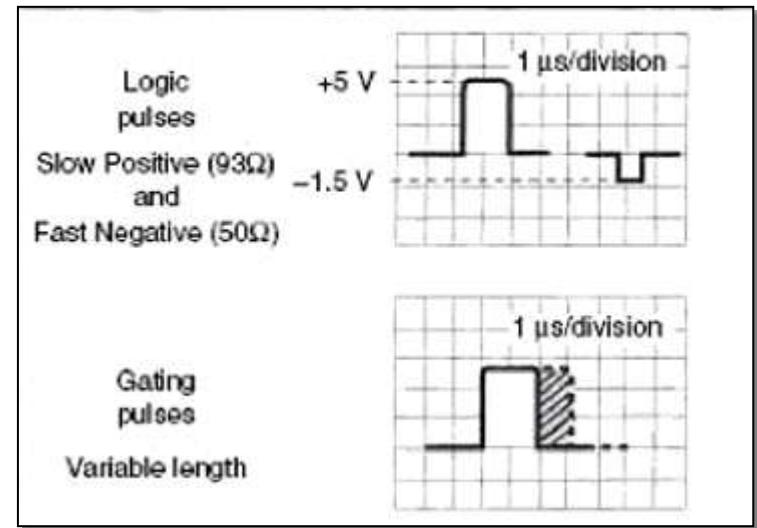
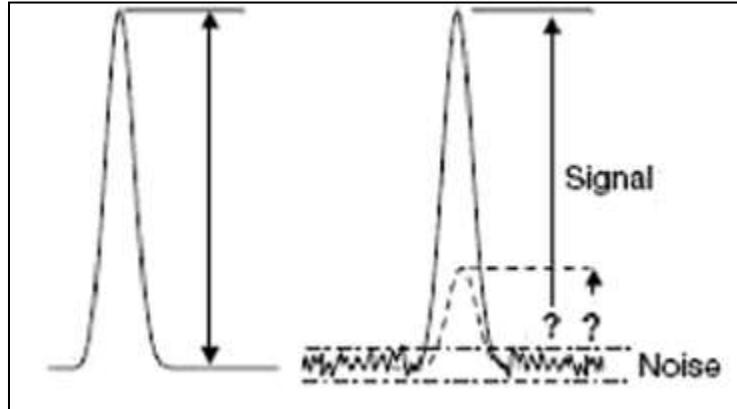
→ Adjust analog and logic electronics

Analog Plus Digital Circuitry

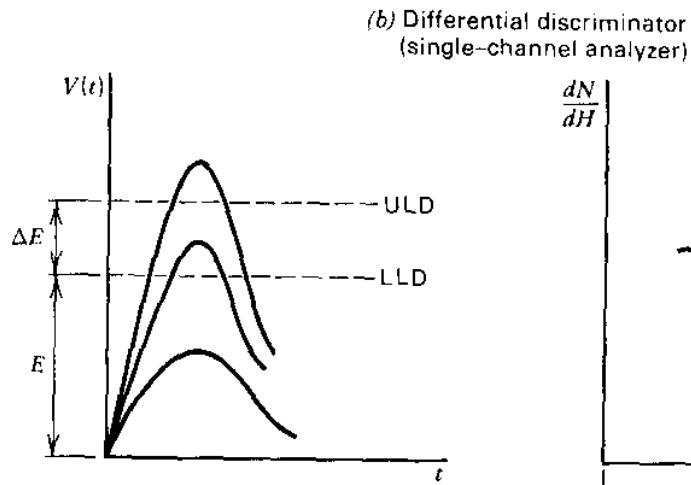
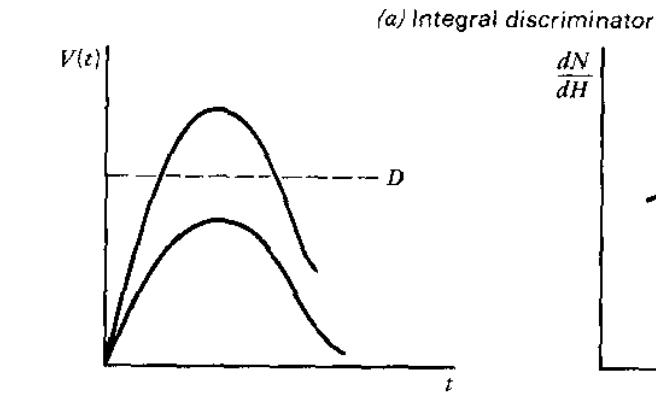
Analog (slow) circuit → proportional image detector output signal



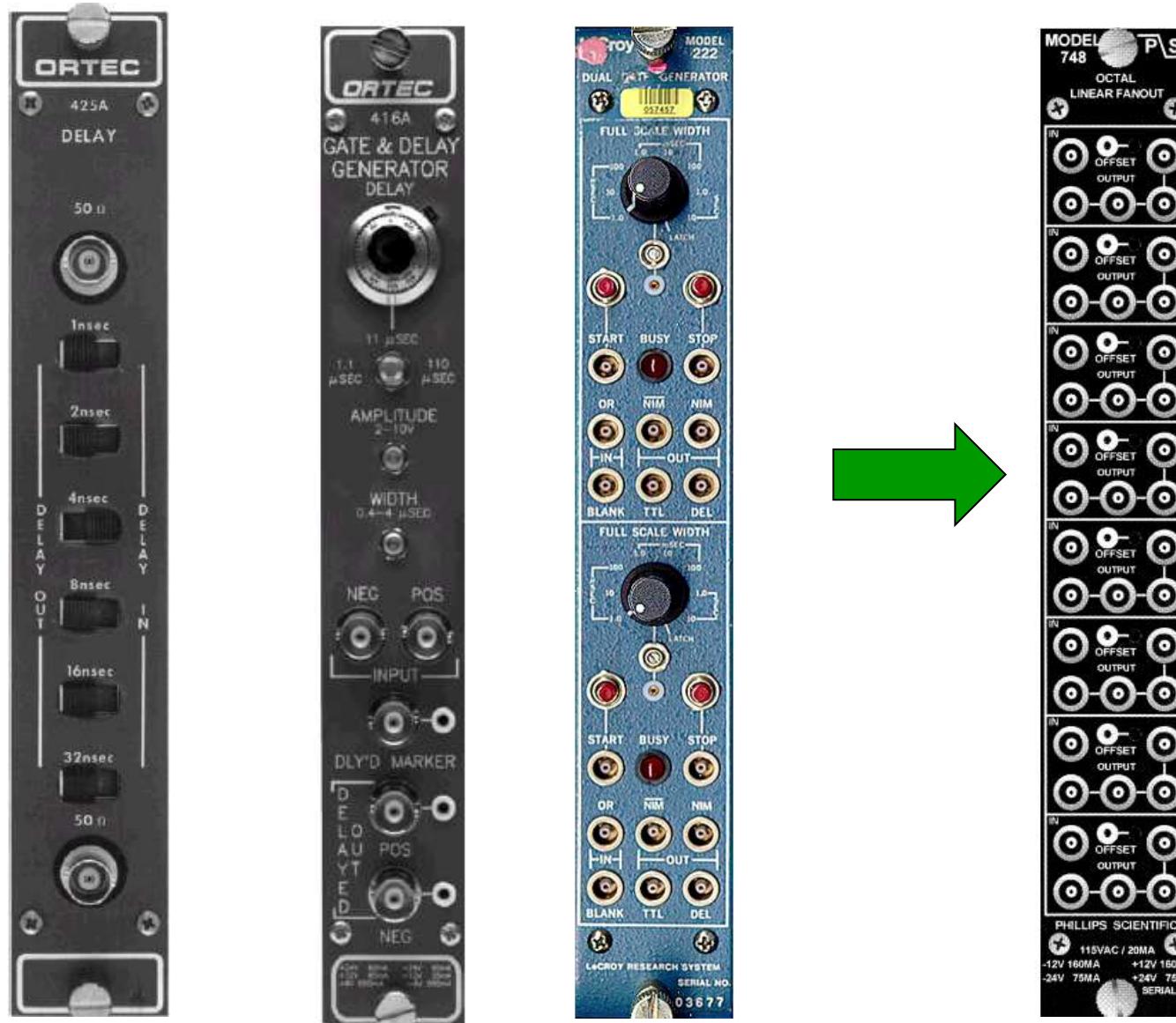
Digital (fast) circuit → yes/no information on signal presence



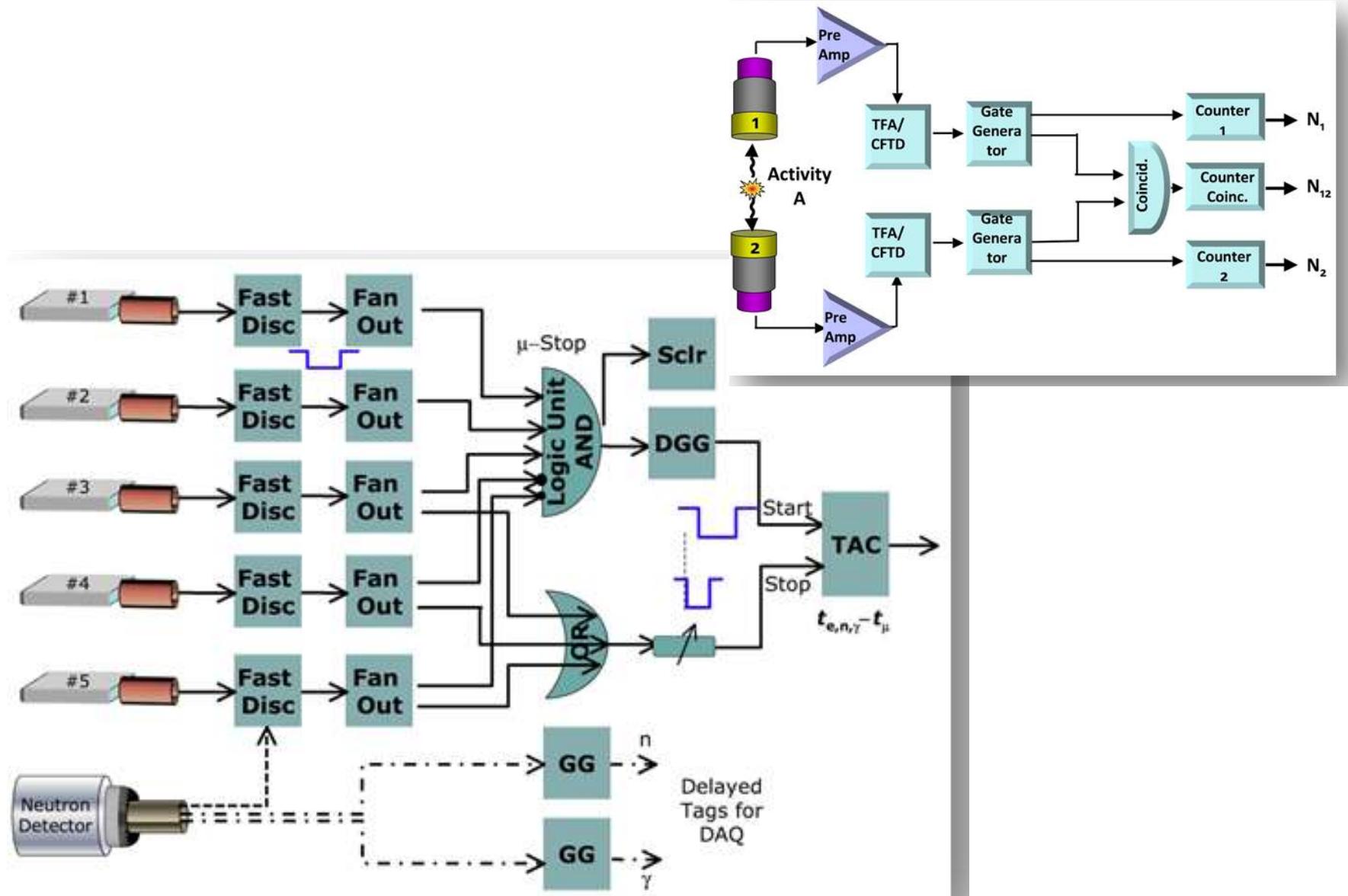
Single Channel Analyzer



Digital Pulse Shaping: Gate and Delay Generators

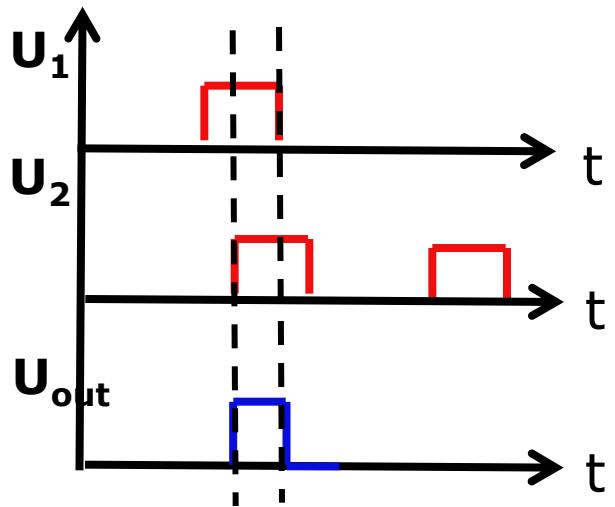
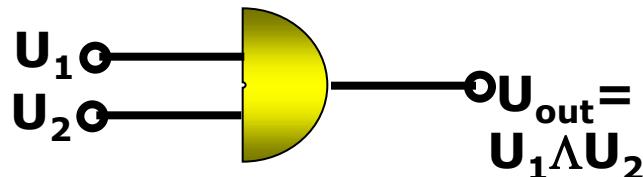


Digital Logic Circuits

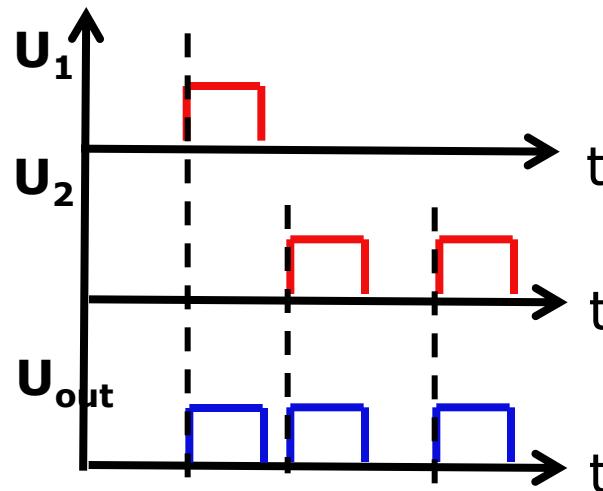
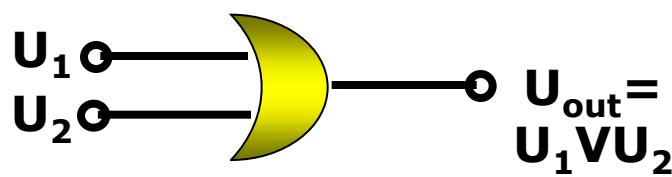


Logic Modules

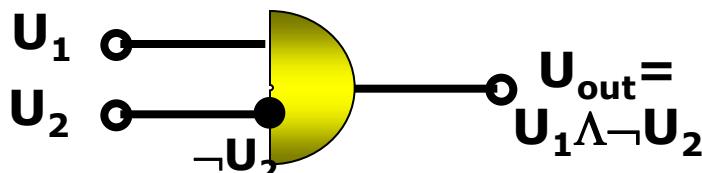
Overlap Coincidence



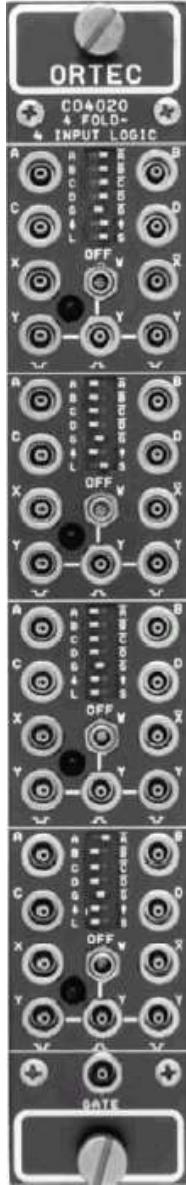
Or (inclusive)



For fast timing:
use fast negative
logic



Anti-Coincidence



Input Logic Switches (A/OFF/A↓ , B/OFF/B↓ , C/OFF/C↓ , D/OFF/D↓ , AND G/OFF/G↓) As defined in Fig. 1, these switches select variations of the following basic logic functions.

In the OFF position, the state of that input is ignored. With switches set to the A, B, C, D, and G positions, the module performs the OR function at the X↓ output.

$$X \downarrow = A + B + C + D + G$$

Setting the switches to the A↓ , B↓ , C↓ , D↓ , and G↓ positions provide the AND (coincidence) function at the X↓ output.

$$X \downarrow = A \cdot B \cdot C \cdot D \cdot G$$

Changing the G↓ switch to G implements the common-gate veto (anticoincidence).

$$X \downarrow = A \cdot B \cdot C \cdot D \cdot G \downarrow$$

See Fig. 1 to determine other possible logic

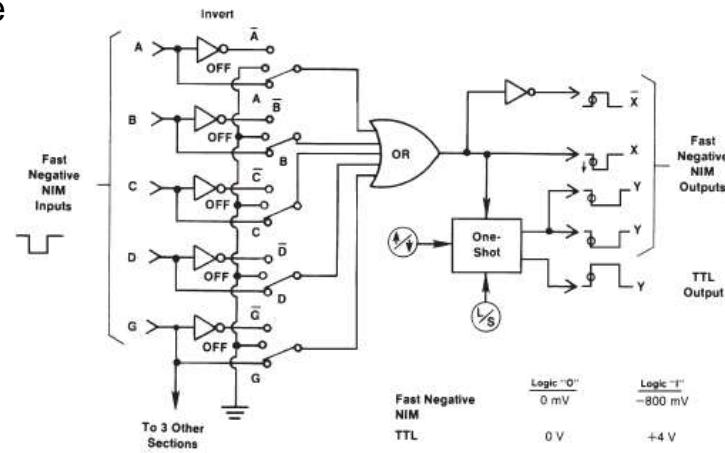
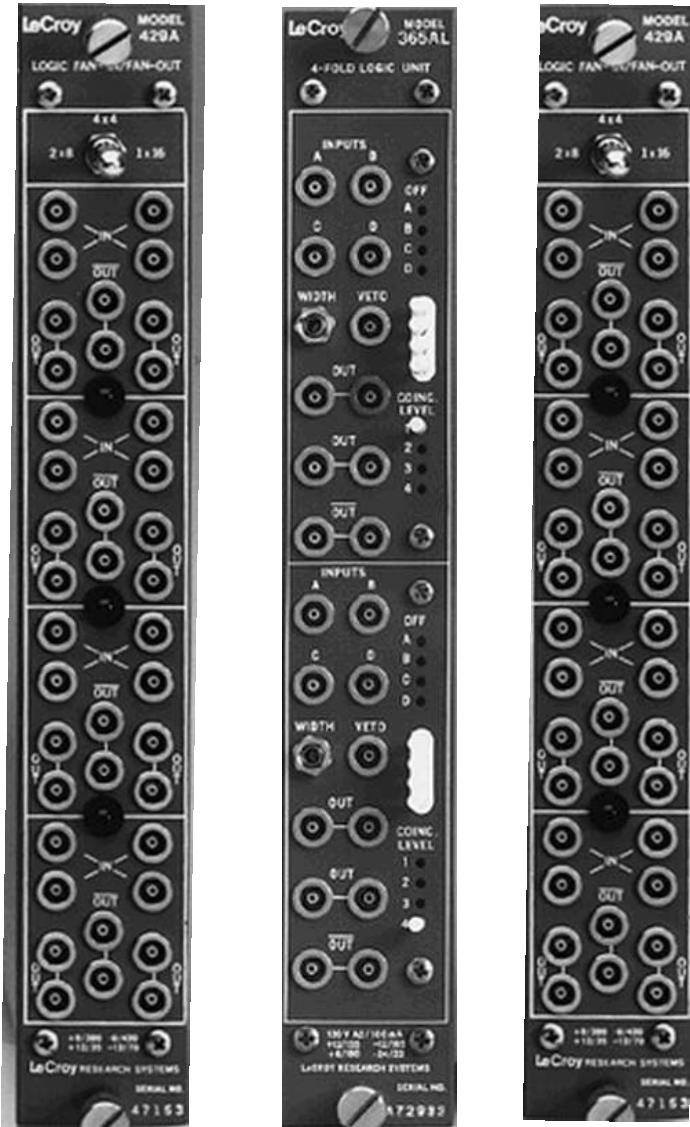
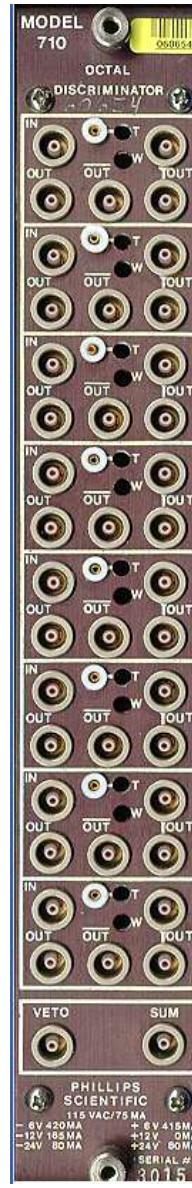
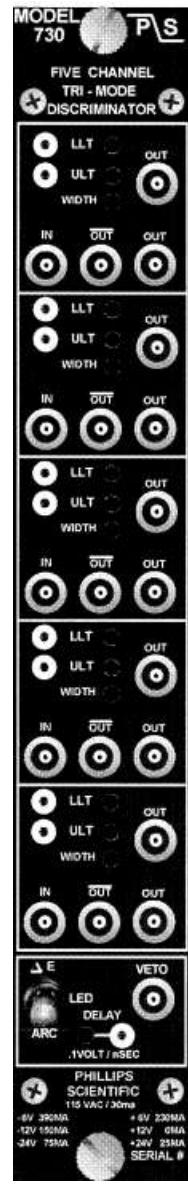
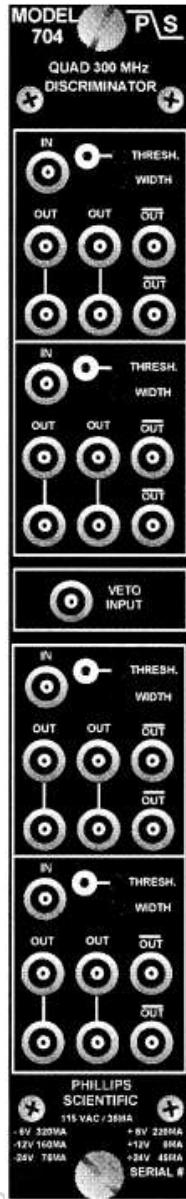
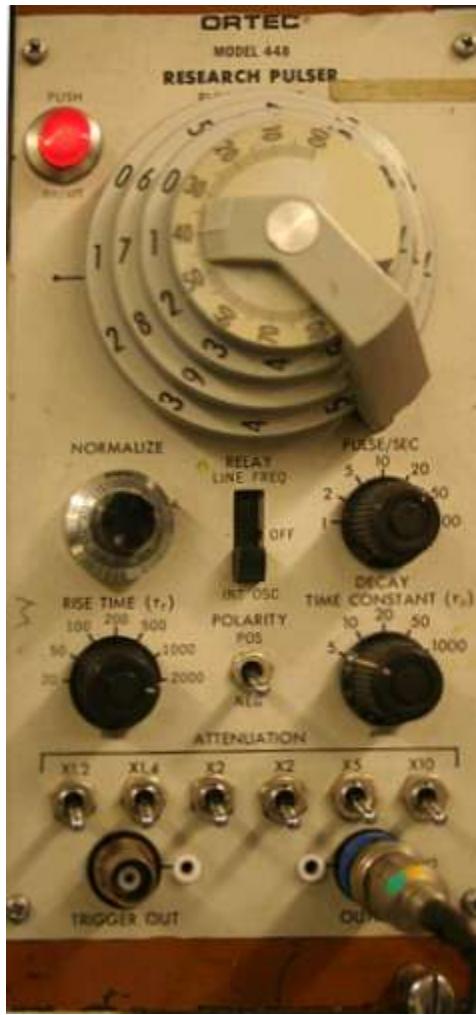
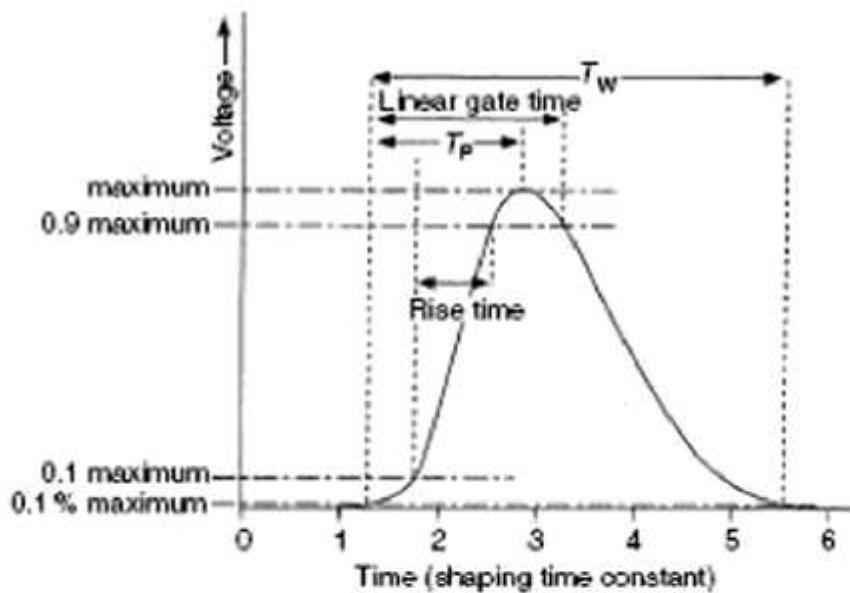


Fig. 1. Block Diagram of the Model CO4020 Logic Unit.



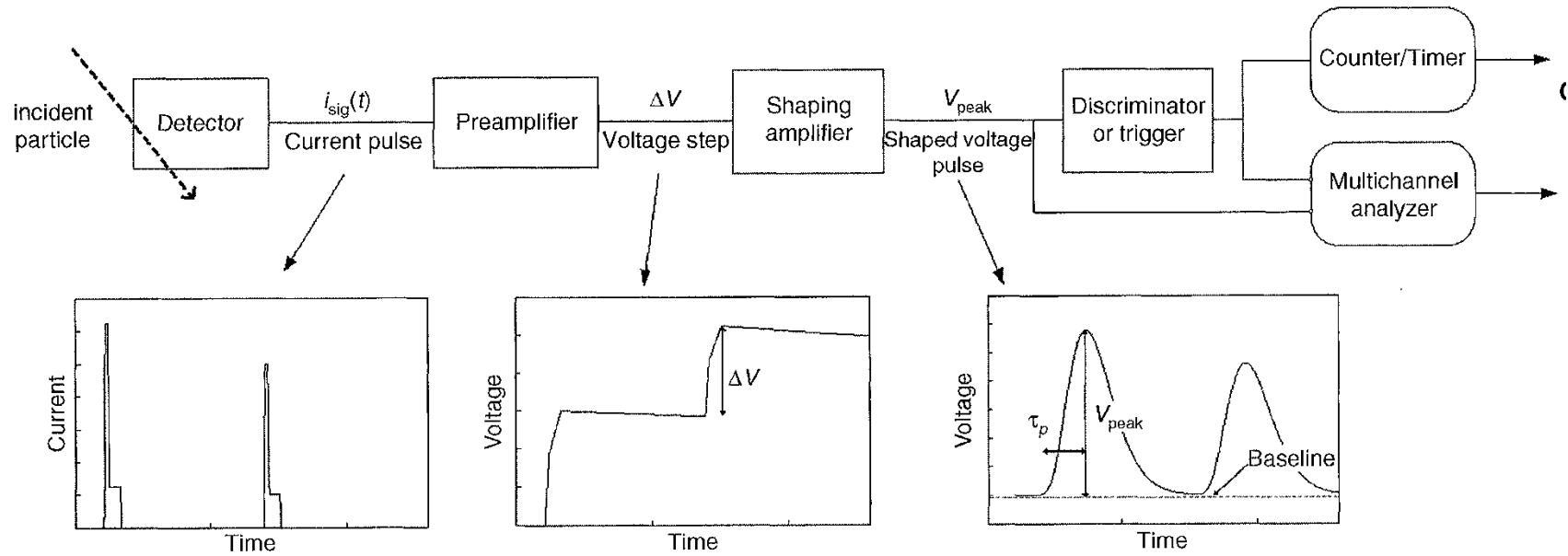
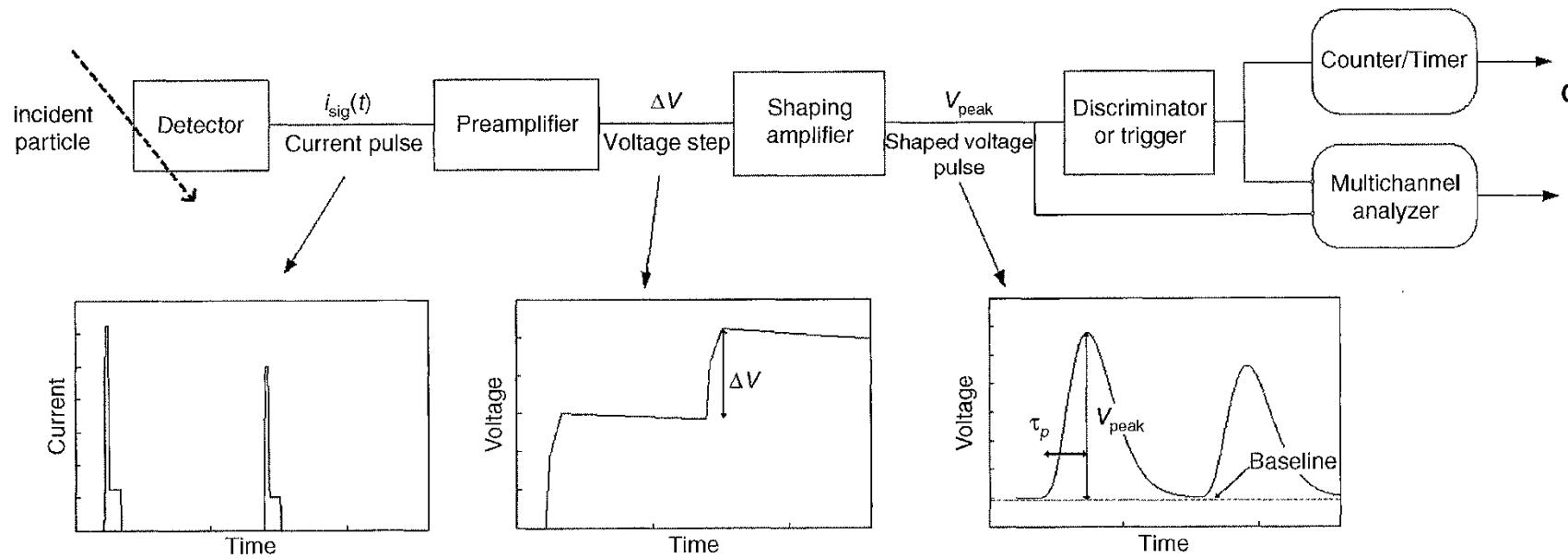


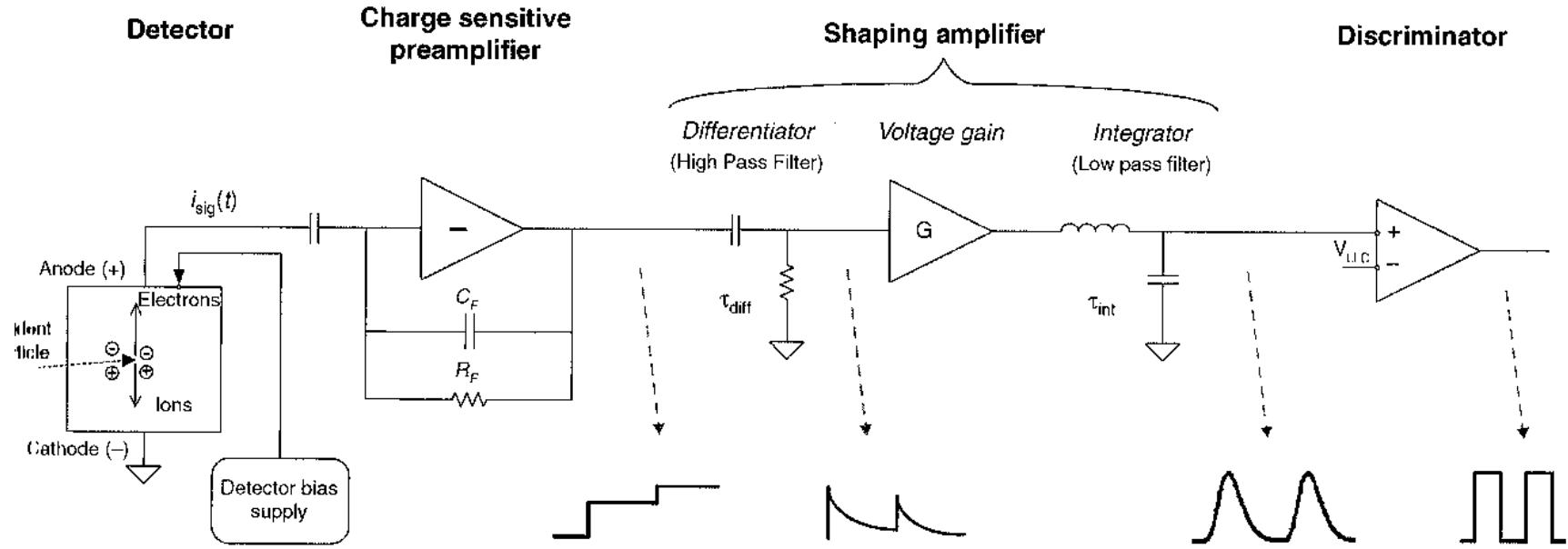


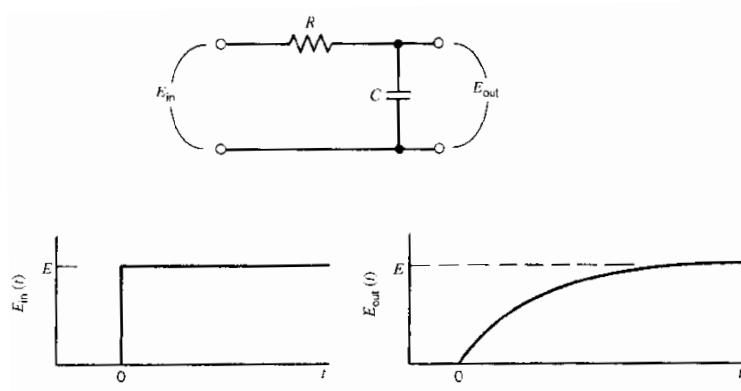
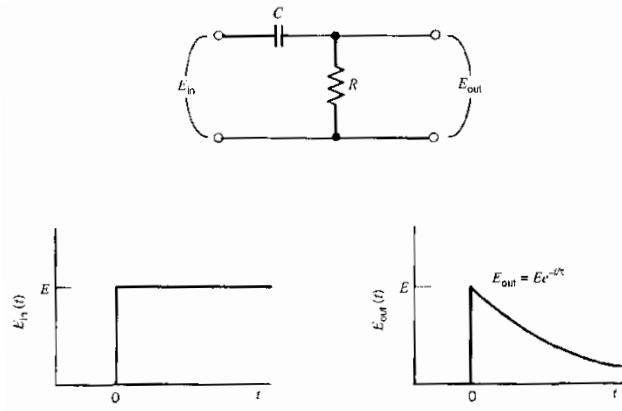


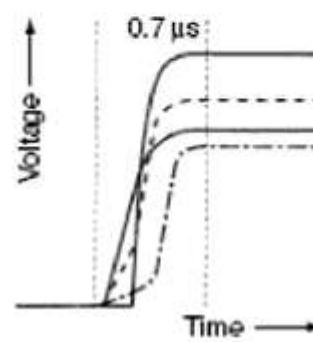
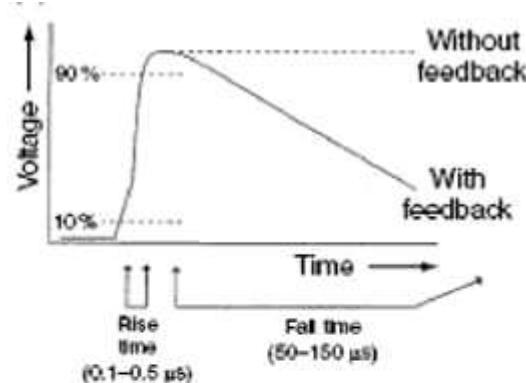
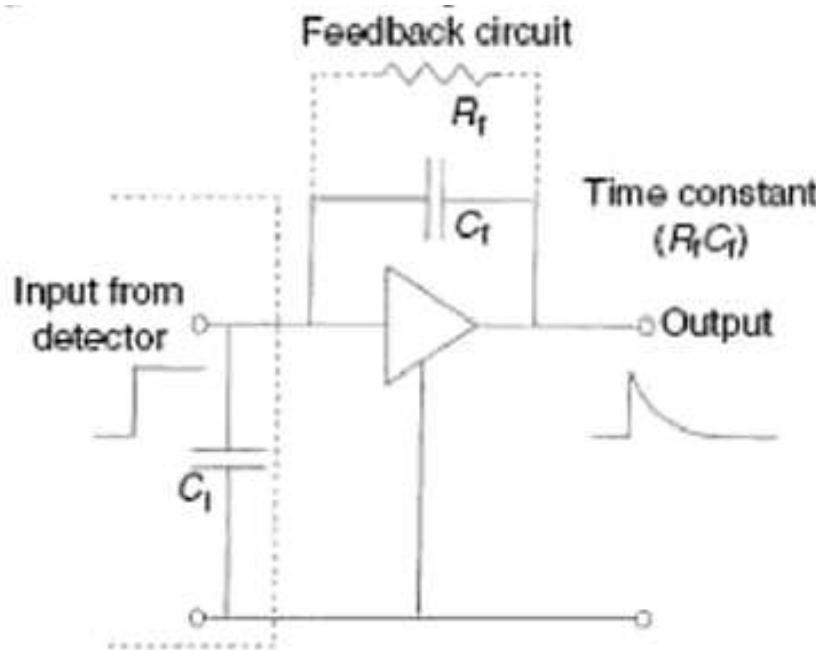
Measured timing factors for semi-Gaussian output pulses

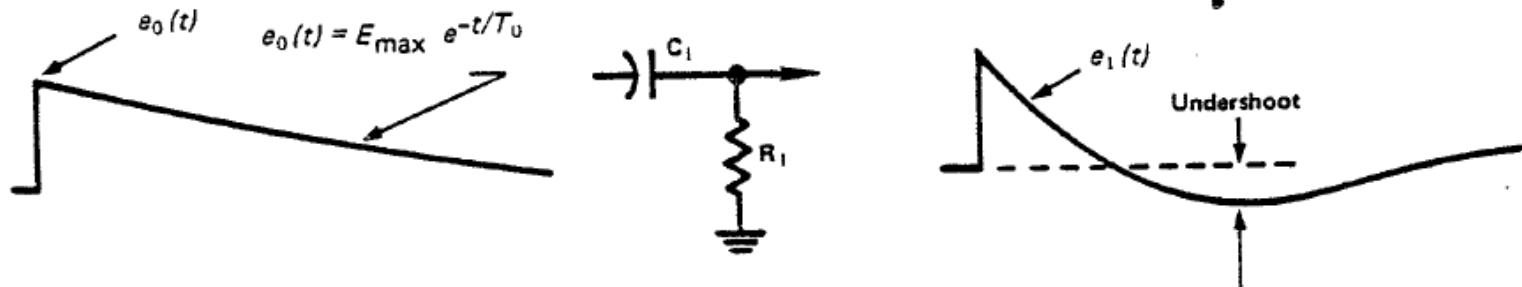
Factor	Time interval	Symbol	Time ^a
Rise time	0.1 to 0.9 of pulse maximum	—	1.26 + 0.05
Peaking time	threshold ^b to maximum	T_p	2.1 + 0.1
Linear gate time	threshold to 0.9 of max. beyond max.	T_{LG}	2.6 + 0.2
Width	threshold to threshold	T_w	5.6 + 0.5











Charge loop output \times First differentiate network = Differentiated pulse with undershoot

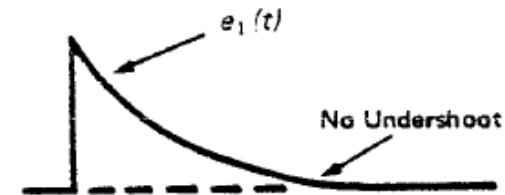
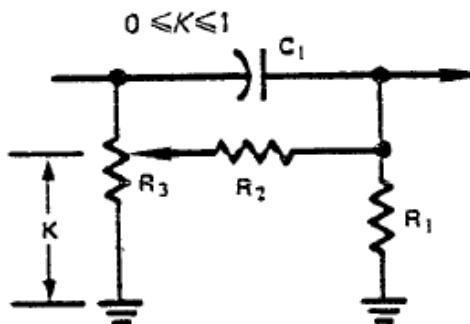
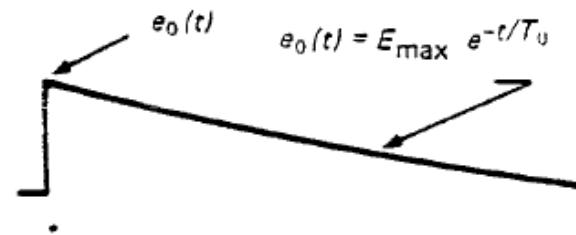
:

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$$E_{\max} e^{-t/T_0} \times G(t) = e_1(t).$$

$$E_{\max} \frac{1}{s + \frac{1}{T_0}} \times \frac{s}{s + \frac{1}{R_1 C_1}} = E_1(s) \text{ (Laplace transform).}$$

$$\frac{E_{\max}}{T_0 - T_1} T_0 e^{-t/T_0} - T_1 e^{-t/T_0} = e_1(t), \text{ where } T_1 = R_1 C_1.$$



Charge loop output \times Pole-zero cancelled differentiator network = Differentiated pulse without undershoot

Pole zero cancel by letting

$$s + \frac{1}{T_0} = s + \frac{K}{R_2 C_1}$$

or

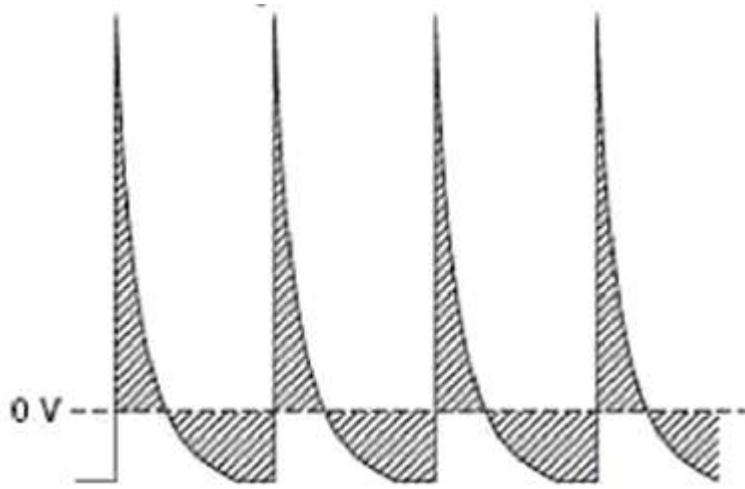
$$\frac{E_{\max}}{s + \frac{R_1 + R_2}{R_1 R_2 C_1}} = \frac{E_{\max}}{s + \frac{1}{R_p C_1}} = E_1(s), \text{ where } R_p = \frac{R_1 R_2}{R_1 + R_2}$$

$$E_{\max} e^{-t/R_p C_1} = e_1(t)$$

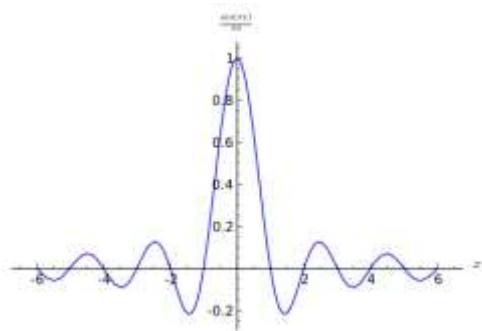
$$E_{\max} \frac{1}{s + \frac{1}{T_0}} \times \frac{s + \frac{K}{R_2 C_1}}{s + \frac{R_1 + R_2}{R_1 R_2 C_1}} = E_1(s). \text{ (Laplace transform).}$$

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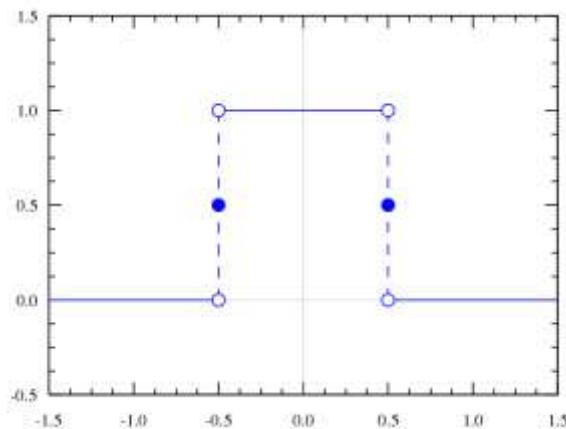
Fig. 1.2. Differentiation in a Pole-Zero Cancelled Amplifier.



Time Dependent Electronic Signals



Function	Fourier transform unitary, ordinary frequency	Fourier transform unitary, angular frequency
$f(x)$	$\hat{f}(\xi) = \int_{-\infty}^{\infty} f(x)e^{-2\pi i x \xi} dx$	$\hat{f}(\omega) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} f(x)e^{-i\omega x} dx$



$$f(\varpi) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{+\infty} g(t) e^{i\varpi t} dt$$

$$\hat{f}(\omega) = \int_{\mathbb{R}^n} f(x) e^{-i\omega x} dx.$$

Under this convention, the inverse transform becomes:

$$f(x) = \frac{1}{(2\pi)^n} \int_{\mathbb{R}^n} \hat{f}(\omega) e^{i\omega x} d\omega.$$

