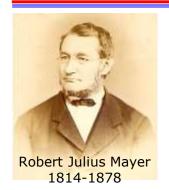


# Agenda

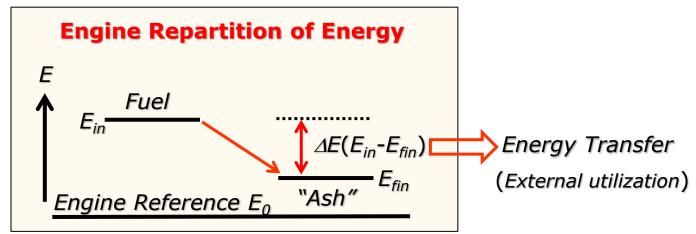
#### Energy conservation, conversion, and transformation

- Potential energy, kinetic energy, work, and power
   Variable force, chemical rearrangement energy (Enthalpy)
   Examples
- Kinetic energy transfer,
   Dissipation, randomization and spontaneous processes
   Examples of thermal motion, Maxwell-Boltzmann distribution
- Electricity and Electromagnetic Power
   Electric fields and currents, metallic and semiconductors
   Magnetic induction
   AC circuits
- Thermodynamics principles and applications
   First Law & Second Law of Thermodynamics, Entropy
   Transfer of thermal energy (heat)
   Conduction, convection, radiation (cooling)
   Internal energy, equivalence of work and heat

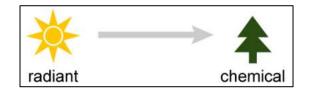
# Schematic of Human Energy Utilization



Conservation of Energy = 1<sup>st</sup> Law of Thermodynamics (TD) Energy in an isolated system can never be created or destroyed. It can only be transformed.

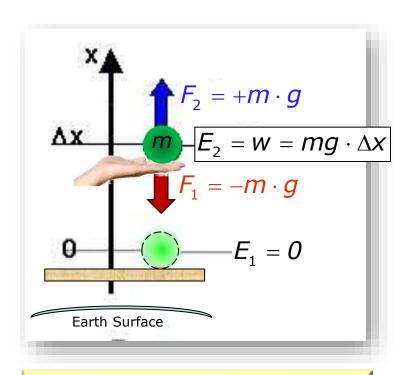


Examples For Energy Conversion





# Mechanical Work & Energy: Weightlifting



Only differences  $\Delta E$  in energy E are measureable  $\rightarrow$  arbitrary energy-zero, E=0.

#### Newton's Law→ Motion of massive bodies:

Balancing gravitational force  $F_1$  requires an equal force  $F_2$  in the opposite direction.

$$\vec{F}_2 = -\vec{F}_1 = -m \cdot g$$

Applying  $F_2$  over an altitude change  $\Delta x$  requires work w

$$W = +F_2 \cdot \Delta X = -F_1 \cdot \Delta X = m \cdot g \cdot \Delta X$$

This increases the intrinsic (potential) energy of the body (= system) by

$$\Delta E = m \cdot g \cdot \Delta X \rightarrow W \equiv \Delta E$$

If the work  $\boldsymbol{w}$  is done during time  $\Delta t$ , the mean power applied is

$$\Delta P = \Delta E/\Delta t = m \cdot g \cdot (\Delta x/\Delta t)$$

The body gains, as internal energy, the difference in gravitational potential energies at different heights x. Body can do work  $w=-mg\Delta x$ .

### Numerical Example

**Q:** What is the potential energy (SI units) gained by a body of mass  $m = 1 \ kg$  lifted vertically up from a table by a distance h = 1m?

**A:** The force resisting the motion of the body is the gravitational force (downwards is the *negative h direction*)

$$F_a = -m \cdot g = -1kg \cdot 9.81 \, m/s^2 = -9.81 \, N$$
 unit

To lift the body requires a *force F upwards* of the magnitude 9.81 N.

This force  $F = -F_g = +9.81 N$ , applied over the distance of 1m does

the work 
$$W = F \cdot 1m = 9.81 Nm = 9.81 J = 6.12 \cdot 10^{19} eV > 0$$

**Q:** If this work is done within 1 second, what is the power P exerted?

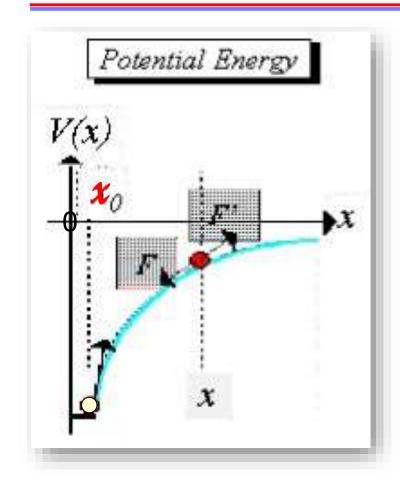
A: 
$$P = w/1s = 9.81 \ J/s = 9.81W \ (Watt)$$

**Q:** If the body is then dropped from its 1-m height, what is its velocity hitting the table (h=0)?

$$W = 9.81J = 0.5 \cdot m \cdot v^2 = 0.5kg \cdot v^2 \rightarrow v = \sqrt{9.81Nm/0.5kg} = 4.4 \, m/s$$

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# Work Against a Variable Force



Variable force F'(x), differential work: Sum over (infinitely) many differentials dw

Lifting: 
$$dw = F'(x) \cdot dx = -F(x) \cdot dx > 0$$

→ Total work **done on** particle in terms of potential energy difference:

$$\mathbf{w} = \int_{x_0}^{x} dw(x') = \int_{x_0}^{x} F'(x') \cdot dx' = -\int_{x_0}^{x} F(x') \cdot dx' > \mathbf{0}$$

$$W = -\int_{x_0}^{x} F(x') \cdot dx' = \int_{x_0}^{x} \frac{dV(x')}{dx'} \cdot dx' = V(x) - V(x_0) = \Delta V$$

In 3D components: 
$$F \to \vec{F} = \begin{pmatrix} F_x \\ F_y \\ F_z \end{pmatrix}$$
;  $X \to \vec{r} = \begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$ 

$$W = -\int_{\vec{r}_0}^{\vec{r}} \vec{F}(\vec{r}) \cdot d\vec{r} = \int_{\vec{r}_0}^{\vec{r}} \vec{\nabla} V(\vec{r}) \cdot d\vec{r} = V(\vec{r}) - V(\vec{r}_0)$$

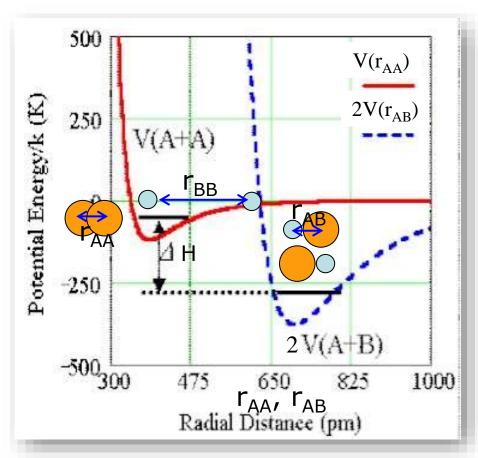
Force = Negative gradient:

$$F(x) = -\frac{dV(x)}{dx} \rightarrow 3D: \qquad \vec{F}(\vec{r}) = -\vec{\nabla}V(\vec{r}) = -\frac{dV(\vec{r})/dx}{dV(\vec{r})/dz}$$

Del or Nabla Operator

### Energy Gain in Chemical Configuration Changes

Example: Covalent bonding (Lennard-Jones potential)



Consider schematic reaction between one bound molecule  $A_2$  and 2 unbound atoms B forming 2 bound molecules AB:

$$A_2$$
+ 2B  $\rightarrow$  2AB (+  $\triangle$ H)

Enthalpy  $\Delta H < 0$ : energy released from the molecular system (2**AB**) Since B are individual atoms and not bound together,  $V(B)=V_{B+B}=0$ .

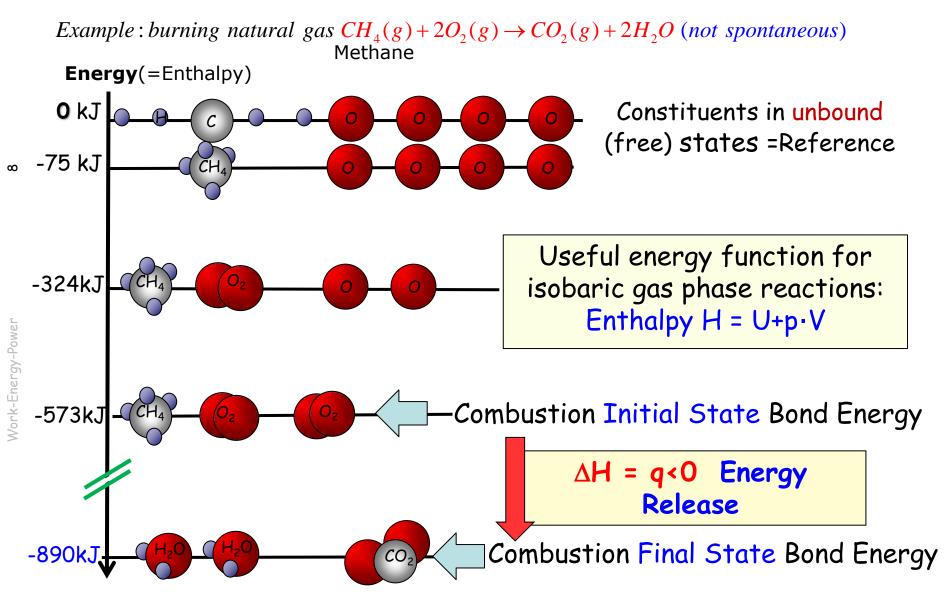
Reaction takes place if

$$2V_{A+B} < V_{A+A} + V_{BB} = V_{A2}$$

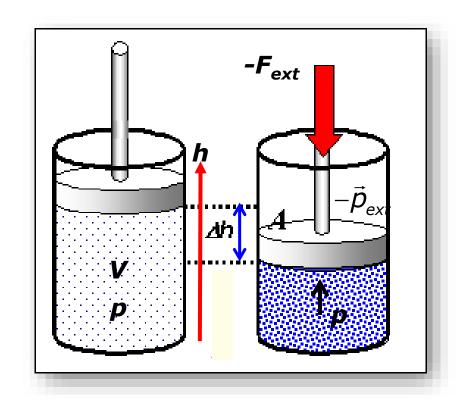
Reaction is exo-thermic (final system is more strongly bound).

Rearrangement of individual constituents of ensemble of atoms and molecules is associated with changes in interaction potential (bonding) energy.

# Example: Bond Changes in Combustion



## Kinetic Energy Changes in Compression



Gas=equilibrated system of independent particles moving in random directions.

Compression of a gas volume V with a constant force F (e.g., weight) on a constant area A:

⇒ Pressure p = Force F/Area A,

at  $p = p_{ext} = \text{const.}$ (external, not internal)  $-F_{ext}$ 

$$p = \frac{-F_{ext}}{A} = p_{ext} \rightarrow \Delta V = A \cdot \Delta h < 0$$

Compression work done on system

$$w = -F_{ext} \cdot \Delta h = -(p_{ext} \cdot A) \cdot \Delta h = -p_{ext} \cdot \Delta V > 0$$

**Sign Convention**: Compressional work on a gas volume (=system) increases the internal energy  $\boldsymbol{E}$  of the gas .

Therefore, work w > 0 is counted as positive (done on gas).

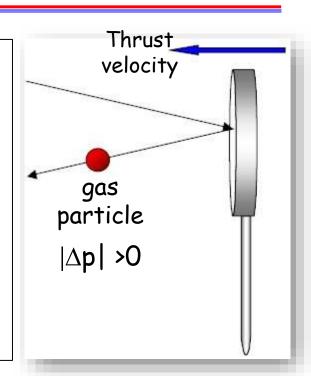
**Q:** How can we measure the gas pressure?

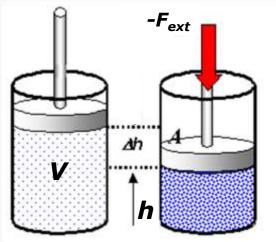
Q: What happens to the piston, what is the pressure p inside the gas volume?

## Compression Work as Energy Transfer



Energy and momentum are transferred to gas particles hit by a (collectively) moving piston, depending on the relative velocity of piston and gas particle.



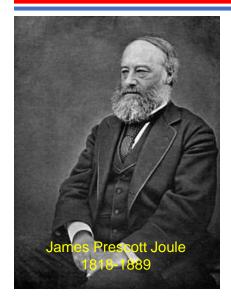


The effect is similar to that driving a tennis ball with a racket.

Thermally insolated system (cylinder with gas)

Compressed gas has more energy in random motion than before. Transfer collective → random motion = dissipation of collective energy into heat.

# Mechanical Equivalent of Heat

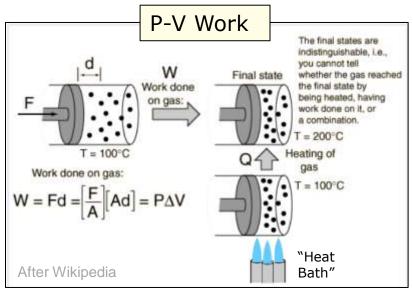


"An Experimental
Enquiry Concerning the
Source of the Heat which
is Excited by Friction",
(1798), Philosophical
Transactions of the
Royal Society p. 102

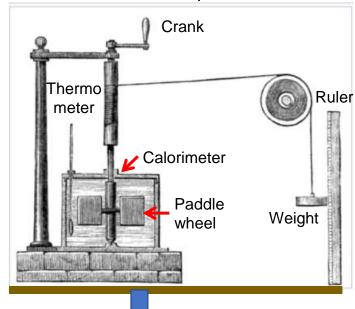
Work 
$$W \propto Q$$
 Heat  

$$\Rightarrow W = JQ$$

$$\Rightarrow J = \frac{W}{Q}$$



#### Joule's experiment



 $J=4.186\ kJ/kcal$ 

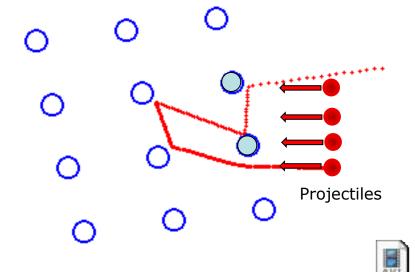
Specific heat  $\rightarrow$  Energy( $\triangle T$ ):  $q = \mathbf{C} \cdot \triangle \mathbf{T}$ 

Heat energy  $\mathbf{q}$  required for heating 1g material by  $\Delta T = 1^{\circ}C$ 

of  $H_2O: C_V(...) \approx (4.17-4.22) J/(g \cdot {}^{\circ}C)$ 

### Energy Dissipation (Randomization)

Multiple Scattering @ Fixed Lattice



A lattice of heavy (M) bound atoms or ions is hit by fast projectiles  $(m \ll M)$ .

A number "projectile" particles enter the system at various initial conditions: positions from the right with identical momenta (e.g., kicked by racket).

Depending on how and where the first lattice particle is hit, the next few collisions and their momentum and energy transfers change.

Lattice\_Scattering.avi

The result is a random pattern of projectile deflections, momenta and energies. The particles hit by the projectiles are also accelerated and deflected to various extents. They themselves become projectiles and collide with other gas particles. In this fashion, the energy of the projectile is dissipated over all particles in the system.

Collisions with unbound, moving **gas** particles are "much more" random than collisions with a periodic solid-sate lattice structure. More complex structures arise naturally (spontaneously) via collisions between particles.

#### Thermal Motion in Solids



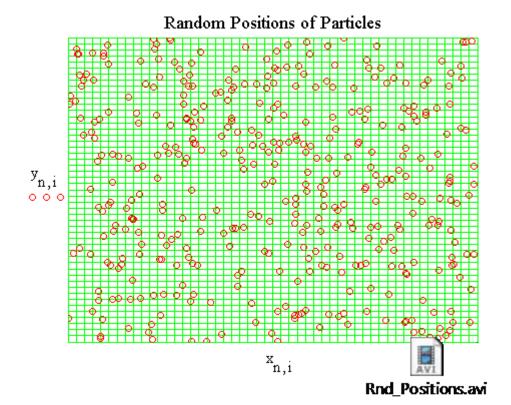
The individual constituents (atoms or ions) of an excited lattice have on average the same thermal energy. If one increases this average energy by introducing energy from the surroundings, the displacements of the particles increase.

At higher excitations, the structure begins to disappear, the lattice is "melting", becomes a liquid and, eventually, a gas.

The average kinetic energy of each particle is known as "temperature T'' (units of  $k_B$ )

 $\langle \varepsilon \rangle = (1/2) \cdot k_B T$  per particle per degree of freedom

# Random (Thermal) Motion in Space



Example: Motion in two dimensions of 300 non-interacting (ideal-gas) particles.

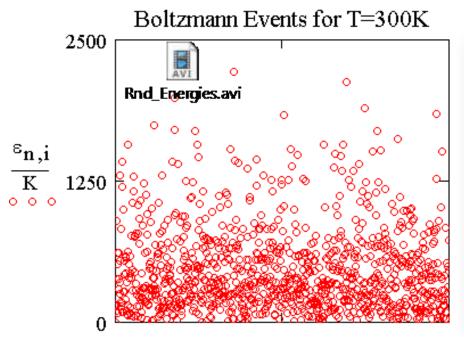
All particles move in random directions because of multiple collisions, which actually do occur but are not explicitly treated here.

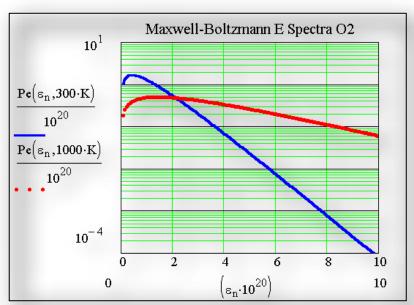
Every particle visits every one of the energetically equivalent cells.

**Contrast: Collective motion.** 

Particles in a gas move in different directions and at different speeds, colliding with one another often. Eventually, their positions at any given time are random. All available (accessible) space is visited by all particles, in due time. → Ergodic Theorem

### Gases in Randomized State (Thermal Equilibrium)



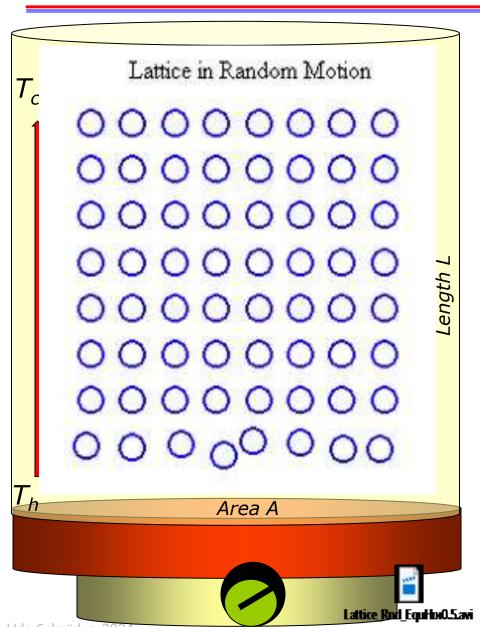


$$P(\varepsilon,T) = \frac{dN}{d\varepsilon} \propto \sqrt{\varepsilon} \cdot e^{-\frac{\varepsilon}{k_BT}}$$

The particles in a gas collide continuously, all the time. In these collisions, different momentum and energy transfers occur, depending on whether the collisions are grazing, head on, or in-between. This leads to a randomly fluctuating ("thermal") "Maxwell-Boltzmann" kinetic-energy spectrum.

(An ideal gas only has internal kinetic energy, no potential energy since no interactions)

# Conduction of Thermal Energy in Solids



External energy and/or density disturbances propagate through its volume V, e.g., its solid lattice.

$$\frac{dq}{dt} = -\kappa A \frac{\left(T_c - T_h\right)}{L} \rightarrow conductivity \ \kappa$$
$$3D: \ \vec{j}_q = \frac{d\vec{q}}{A \cdot dt} = -\kappa \cdot \vec{\nabla} T$$

**Energy flow: hot** → **cold** 

System expands in spatial dimensions

$$dV = V \cdot (1 + \alpha \cdot dT)$$
  
 $\rightarrow \alpha = volume \ expansion \ coeff$ 

Systems at any temperature emit thermal radiation (IR photons), which can be absorbed (possibly re-emitted) by objects in the environment.

Stefan-Boltzmann Law

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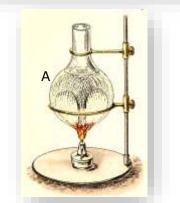
Heat conduction, flux=current density through area A

$$j_q = (dQ/dt) / A$$

Fourier's Law: 
$$\vec{j}_q = -\kappa \cdot \vec{\nabla} T(\vec{r}) = -\kappa \cdot \left( \frac{\partial T}{\partial x} \vec{i} + \frac{\partial T}{\partial y} \vec{j} + \frac{\partial T}{\partial z} \vec{k} \right)$$

Thermal conductivity  $\kappa$  (W/mK)

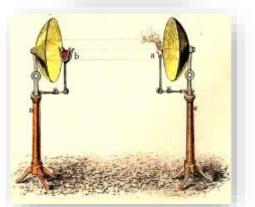
https://www.schoolmykids.com/learn/interactive-periodic-table/thermal-conductivity-of-all-the-elements



Heat convection: Heat transfer via particles (mass flow)

Newton's Law of cooling 
$$\frac{dQ}{dt} = -h \cdot A \cdot (T - T_{ambient})$$

Heat transfer coefficient h ( $W/m^2K$ ); area A



Heat radiation: Heat transfer via elm. photons

Stefan – Boltzmann Law

Radiated thermal flux  $j_Q = \varepsilon \cdot \sigma_{SB} \cdot (T^4 - T_{ambient}^4)$ 

*Emissivity*  $\varepsilon$  (often = 1)

Stefan – Boltzmann constant  $\sigma_{SB} = 5.6703 \cdot 10^{-8} \, W/m^2 K^4$ 

|         | ft lb                | kWh                    | hph                    | Btu                    | Calorie               | Joule               |
|---------|----------------------|------------------------|------------------------|------------------------|-----------------------|---------------------|
| ft lb   | 1                    | $3.766 \times 10^{-7}$ | $5.050 \times 10^{-7}$ | $1.285 \times 10^{-3}$ | 0.324                 | 1.356               |
| kWh     | $2.655 \times 10^6$  | 1                      | 1.341                  | $3.413 \times 10^{3}$  | $8.606 \times 10^{5}$ | $3.6 \times 10^{6}$ |
| hph     | $1.98 \times 10^{6}$ | 0.745                  | 1                      | $2.545 \times 10^{3}$  | $6.416 \times 10^5$   | $2.684 \times 10^6$ |
| Btu     | 778.16               | $2.930 \times 10^{-4}$ | $3.930 \times 10^{-4}$ | 1                      | 252                   | $1.055 \times 10^3$ |
| Calorie | 3.086                | $1.162 \times 10^{-6}$ | $1.558 \times 10^{-6}$ | $3.97 \times 10^{-3}$  | 1                     | 4.184               |
| Joule   | 0.737                | $2.773 \times 10^{-7}$ | $3.725 \times 10^{-7}$ | $9.484 \times 10^{-4}$ | 0.2390                | 1                   |

# End Work/Energy/Power I